



Ice Volumes on Cascade Volcanoes:  
Mount Rainier, Mount Hood,  
Three Sisters, and Mount Shasta

U.S. GEOLOGICAL SURVEY PROFESSIONAL PAPER 1365

**Cover.**—Mount Rainier (as seen from the west) is in some ways representative of all the volcanoes in this study. Each volcano provides a high mountain environment on which the glaciers exist, and which is in turn eroded by forces associated with glaciation. (U.S. Geological Survey photograph.)

ICE VOLUMES ON  
CASCADE VOLCANOES



Aerial photograph of Collier Cone, Oreg. (bottom-center of photograph), a cinder cone similar in eruption characteristics to the Mexican volcano Parícutin. Active between 500 and 2,500 years B.P. (Taylor, 1981, p. 61), the cone erupted between the lateral moraines of Collier Glacier. During the early 1930's, the terminus of Collier Glacier abutted the south flank of Collier Cone, reworking the cinders into the striated pattern visible today (Ruth Keen, Mazamas Mountaineering Club, oral commun., 1984). Williams (1944) reported the presence of glacial moraine interspersed with lava flows around the base of Collier Cone. (U.S. Geological Survey photograph by Austin Post on September 9, 1979.)

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By CAROLYN L. DRIEDGER *and* PAUL M. KENNARD

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U.S. GEOLOGICAL SURVEY PROFESSIONAL PAPER 1365



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## SYMBOLS AND ABBREVIATIONS

<i>Symbol</i>	<i>Name</i>	<i>Symbol</i>	<i>Name</i>
$A$	Surface area	$p$	Path of light
$b$	Slope of bedrock measured from horizontal	$R$	Resistance per unit length
$c$	Speed of light in ice	$t$	Time between arrivals of air and reflected waves on the oscilloscope
$c_o$	Speed of light in a vacuum	$V$	Volume
$CI$	Contour interval	$V^*$	Volume estimation by calculation of basal shear stress
$d$	Transmitter-receiver separation distance	$x$	Distance from antenna feedpoint in meters
$g$	Gravitational acceleration	$\alpha$	Slope of ice measured from horizontal
$h$	Thickness measured perpendicular to the reflecting point on a glacier bed	$l$	Antenna half-length (meters)
$h'$	Vertical distance between the measurement point and the bedrock	$\eta$	Refractive index of ice
$i$	(Subscript) indicates an interval value	$\nu$	Frequency
$k_{1,2,3}$	Coefficients derived from regression analysis	$\rho$	Density of ice
$l$	Glacier length	$\tau$	Basal shear stress
		$\tau^*$	Estimated basal shear stress
		$\psi$	Resistive loading constant (ohms)

# ICE VOLUMES ON CASCADE VOLCANOES: MOUNT RAINIER, MOUNT HOOD, THREE SISTERS, AND MOUNT SHASTA

By CAROLYN L. DRIEDGER and PAUL M. KENNARD

## ABSTRACT

During the eruptions of Mount St. Helens the occurrence of floods and mudflows made apparent the need for predictive water-hazard analysis of other Cascade volcanoes. A basic requirement for such analysis is information about the volumes and distributions of snow and ice on other volcanoes.

A radar unit contained in a backpack was used to make point measurements of ice thickness on major glaciers of Mount Rainier, Wash.; Mount Hood, Oreg.; the Three Sisters, Oreg.; and Mount Shasta, Calif. The measurements were corrected for slope and were used to develop subglacial contour maps from which glacier volumes were measured.

These values were used to develop estimation methods for finding volumes of unmeasured glaciers. These methods require a knowledge of glacier slope, altitude, and area and require an estimation of basal shear stress, each estimate derived by using topographic maps updated by aerial photographs. The estimation methods were found to be accurate within  $\pm 20$  percent on measured glaciers and to be within  $\pm 25$  percent when applied to unmeasured glaciers on the Cascade volcanoes. The estimation methods may be applicable to other temperate glaciers in similar climatic settings.

Areas and volumes of snow and ice are as follows: Mount Rainier, 991 million  $\text{ft}^2$ , 156 billion  $\text{ft}^3$ ; Mount Hood, 145 million  $\text{ft}^2$ , 12 billion  $\text{ft}^3$ ; Three Sisters, 89 million  $\text{ft}^2$ , 6 billion  $\text{ft}^3$ ; and Mount Shasta, 74 million  $\text{ft}^2$ , 5 billion  $\text{ft}^3$ .

The distribution of ice and firn patches within 58 glacierized basins on volcanoes is mapped and listed by altitude and by watershed to facilitate water-hazard analysis.

## INTRODUCTION

The 1980 eruption of Mount St. Helens removed an estimated 4.6 billion  $\text{ft}^3$  of ice and snow from the mountain, aiding the formation of lahars and floods (Brugman and Post, 1981, p. D1). There is evidence of similar glaciovolcanic interactions on other Cascade volcanoes, and man can anticipate such threats during future eruptions. Therefore, determining the volumes of the ice and snow should be useful in assessing the potential hazard from eruptions of individual volcanoes.

Between April and September 1981 an ice-radar system developed by the U.S. Geological Survey was used to determine ice thickness at 177 measurement points on 25 glaciers of Mounts Rainier, Hood, and Shasta and the North, Middle, and South Sisters (collectively referred to here as the Three Sisters, fig. 1). Access to these measurement points was by foot, ski, and helicopter and involved personnel from the Project Office—Glaciology, Tacoma, Wash. The measurements allowed

the preparation of subglacial contour and isopach maps included in this paper, along with the resulting volume calculations. The descriptions of ice-radar operation and methods for data reduction, calculation of glacier volume, and error totals in calculating glacier volume are condensed from a study by Kennard (1983).

## ACKNOWLEDGMENTS

Suzanne Brown, Lee Benda, David Peckham, Melinda Brugman, and others from the U.S. Geological Survey Project Office—Glaciology and from the Cold



FIGURE 1.—Locations of volcanoes studied.

Regions Hydrology Project provided invaluable help during this study. During the 6 months of fieldwork, they aided with radar measurements and surveying and also helped by giving their constant energy and enthusiasm. Success in making measurements in nearly inaccessible places was often due to support by Sue and Anthony Reece of HiLine Helicopters.

Personnel of Mount Rainier National Park and of the Mount Hood, Deschutes, Willamette, and Shasta National Forests cooperated by providing information on mountain conditions and by allowing us to carry out the logistics within these regions.

Dr. Charles Raymond offered valuable insight and support for developing the volume estimation methods.

Paul Kennard organized and coordinated fieldwork for the study. He determined the basal contours for the Mount Rainier and Mount Hood glaciers, developed the volume estimation methods and error analysis discussed here, and prepared the appendix. Carolyn Driedger and Bruce Vaughn determined the basal contours at the Three Sisters and Mount Shasta. They applied the estimation methods to all unmeasured glaciers noted in the study.

Beneficial reviews of the manuscript were made by Dee Molenaar, Bernard Hallet, and Robert Jacobel. William Scott, C. Dan Miller, and Dwight Crandell provided information and sectional reviews in reference to geologic histories and glaciovolcanic relations.

### FIELD MEASUREMENTS

Portable monopulse-radar equipment that could be deployed rapidly from a backpack and antennas applicable to a wide range of ice thickness were needed to complete the work. In the radar operation, separate transmitting and receiving antennas were placed on the ice a known distance apart. An oscilloscope recorded arrival of the transmitted air wave and the wave reflected from the bedrock (fig. 2). Oscilloscope screen output was photographed on self-developing film. The theory and principles of operation of the monopulse radar are described in more detail in the appendix.

As all depth measurements were point measurements, it was necessary to obtain accurate map positions, and, as large ice masses have few features identifiable with certainty on a map, surveying was required on Mount Rainier and Mount Hood. Standard survey procedures were followed for field surveying; a theodolite and an electronic distance-measuring device were used. Because glaciers on the Three Sisters and Mount



FIGURE 2.—Ice radar unit in operation on Diller Glacier on the Middle Sister, Ore. The transmitter and antennas are on the snow. Receiving unit and oscilloscope are operated from top of backpack in photo. (U.S. Geological Survey photograph by Carolyn Driedger in September 1981.)

Shasta are generally smaller than those on Mounts Hood and Rainier, locations could be determined adequately with a pocket transit and aerial photos.

Measurement points were selected to give representative coverage of the major ice bodies on each mountain, as well as on some smaller glaciers and patches of perennial snow (firn), referred to in this paper as snow patches.

The number of measurement points on each glacier ranged from 1 to 31. The ultimate number and locations were determined by weather, avalanche and ice-fall conditions, suitable helicopter landing areas, and the ability to obtain unambiguous bottom-measurement returns. Final data-point locations are shown on plates 1–6.

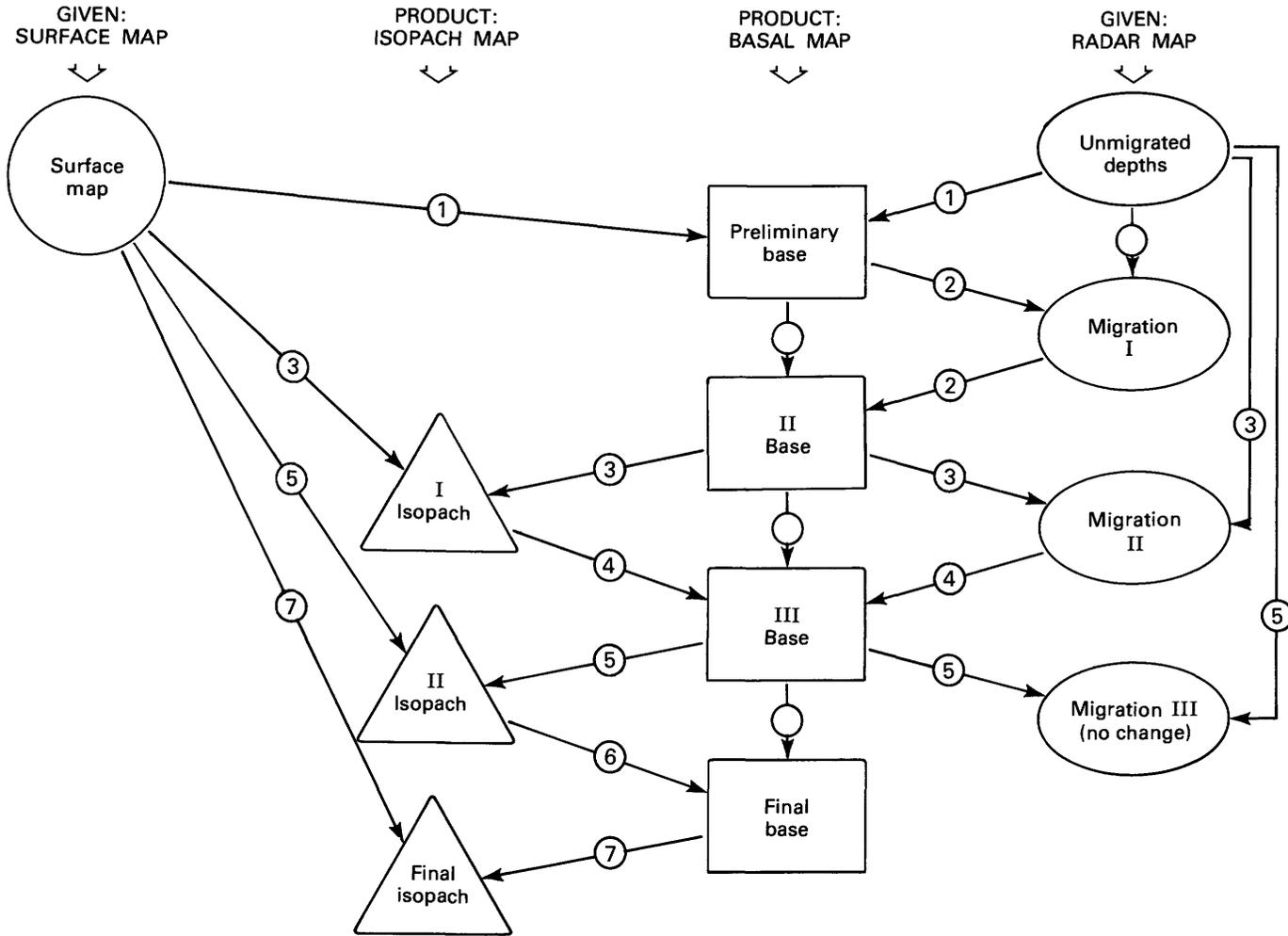


FIGURE 3.—Interactive processes used to produce basal and isopach maps, as in plates 1 through 6 (Kennard, 1983).

**PRIMARY DATA REDUCTION**

The iteration of processes required for developing bedrock and isopach maps is detailed here and is summarized in figure 3. The first step following fieldwork involves finding the ice thickness at each measurement point. Figure 4 shows the geometry of a measurement point and indicates the path of the radar wave between bedrock and the surface. The procedure uses equation 1, where it is assumed that the glacier and bedrock surfaces are planar and the glacier consists only of ice.

Required for the calculation are the separation distance between the pulse source and the receiver ( $d$ ), the time interval between the arrival at the oscilloscope of the air wave and the reflected wave ( $t$ ), the speed of light in a vacuum ( $c_0$ ), and the refractive index of ice ( $\eta$ ). An apparent thickness ( $h$ ) was calculated at each point by

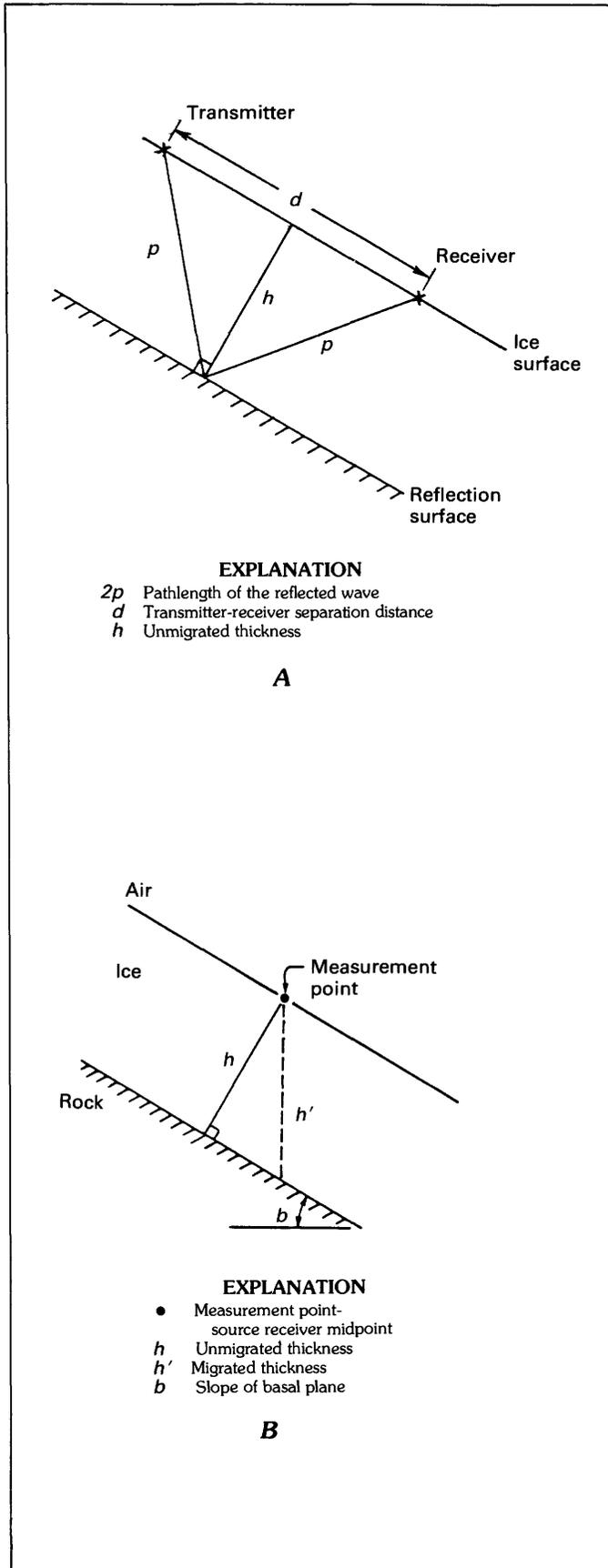
$$h = \frac{\left[ \left( \frac{c_0}{\eta} t + \frac{d}{\eta} \right)^2 - d^2 \right]^{1/2}}{2} \quad (1)$$

Computations showed that correcting for the differences in the refractive index on ice, firn, and snow had an effect of less than two and a half percent on glacier-thickness determinations because the layers of snow and firn are thin. In the data reduction, the presence of snow and firn were disregarded and the total thickness at each measurement point was assumed to be ice. Any debris-laden layer at the base of the ice was assumed to be a reflecting surface and was considered glacier bed.

Thickness measurements were considered accurate to  $\pm 3.0$  percent for a typical data point, including photograph reading errors and errors owing to neglecting the presence of snow and firn. These apparent point thicknesses, together with geological interpretation, were used to develop subglacial contour maps, referred to hereafter as basal maps.

**USE OF MEASURING POINT MIGRATION TO CORRECT FOR BEDROCK SLOPE**

Initially, the basal altitude below each measured point was assumed to be the surface altitude less the



apparent thickness (fig. 4A). However, because radar reflects off the nearest rock surface, a migration correction is required to find the true thickness vertically beneath each point.

The ice-depth equation (eq. 1) defines an ellipsoid, the radar source and receiver being at the respective foci. Theoretically, the reflection point could lie anywhere on this surface. If the measurements were taken within a distance of each other equal to an ice depth, a true reflection surface could be constructed by the envelope of the intersections of the various ellipsoids. In all but one instance, measurements were too far apart to allow construction of an envelope, and a geometrical migration scheme was required to determine the basal geometry.

For example, with a measurement made on steep ice in the middle of a glacier, the reflection point would most likely come from rock at an angle to the point and not directly below it (fig. 4B). Similarly, a sounding taken on a flat section of glacier near the valley wall would most likely be reflected from the side rather than from directly below. Because a map projection of the glacier was used, knowledge of the vertical distance between the measuring point and the bedrock ( $h'$ ) was required. This was calculated by

$$h' = \frac{h}{\cos b} \quad (2)$$

where  $b$  was measured along the bedrock slope and through the measurement point.

For purposes of migration only, it is assumed in the above equation that the transmitted radio wave is spherical, hence negligible error for typical readings is introduced. Using the basal map developed with apparent thicknesses, we computed angle  $b$  by measuring the distance between contours along a curve perpendicular to the contours and passing through the measurement point.

The apparent thickness was migrated by using this estimate of basal slope in the immediate measurement area to yield an estimated base elevation directly below each measurement point. This was used to revise the basal contour map; a new basal slope was measured and the process repeated. This migration scheme was iterated, usually three or four times, with changes up to several millimeters at the map scale, until the base elevation value ceased changing. When drawing contours around individual measurement points, the estimated thickness was not expected to apply directly to

◀ FIGURE 4.—A, The location of the transmitter and receiver relative to the bedrock reflection surface. B, Closeup of A that indicates the slope correction necessary for measuring vertical ice thickness rather than distance from the transmitter to the nearest reflection surface (Kennard, 1983).

the base area for more than approximately a distance equal to the ice thickness, though its influence on the contour pattern may have extended farther. If a contour were moved during migration, it was generally necessary to adjust the neighboring contours. Ice-surface features seen on aerial photographs were used as an aid in correctly locating the contours.

#### USE OF MAPS AND PHOTOGRAPHS TO INFER BASAL TOPOGRAPHY

The maps used were the most current U.S. Geological Survey topographic maps available for each area. The Mount Hood, Mount Shasta, and the Three Sisters maps were enlarged to a scale of 1:10,000 and then reduced to 1:20,000 for this publication, and the Mount Rainier map was used at the original scale of 1:24,000 and reduced to 1:48,000 for this publication. Two-hundred-foot contour intervals were used on Mount Rainier and 100-foot intervals were used on the other mountains for ease in determining area and volume by altitude. Observations from photographs were an important part of map development, as they were useful as indicators of basal relief. Where available, some older photographs showing lower ice levels and exposed basal relief were examined (fig. 5).

Field observations and autumn 1980 and 1981 aerial photographs were used to update the maps for current glacier boundaries, termini positions, and perennial snow patch locations. Therefore, the resulting maps and values indicate areas and volumes in autumn, at the end of the ablation season.

#### ICE-SURFACE FEATURES AND THEIR RELATION TO THE BASAL TOPOGRAPHY

It is generally accepted that the surficial topography of a glacier reflects bed topography in diminished complexity, though bed features are reflected more accurately on the surface of thin ice than on thick ice. It is possible through the judicious use of photographs to determine the trend of the basal topography for most glaciers.

Bedrock configurations induce flow regimes recognizable by characteristic crevasse patterns, but care must be taken when using these to infer basal topography. Interpretation of the crevasse patterns is necessary to distinguish between those caused by the shear stress along the valley walls and those caused by local relief along the channel. Local changes in slope or channel width lead to areas of extending and compressing flow. Transverse crevasses tend to define areas of extending flow. In general, extending flow occurs above icefalls, and compressing flow occurs below them. Extending flow commonly occurs in accumulation areas.

Crosshatched crevasse patterns may arise from ice flow over a bed bulge. A reduction of valley wall constraints often leads to splaying crevasses as seen near glacier termini. Generally, crevasses are products of stresses due to local topographic irregularities in the glacier bed, though they may move with the ice from the area in which they formed.

Some surficial features bear no relation to bedrock topography. Wind-caused features and avalanche deposit zones can result in anomalous surface curvature. Convergent or divergent ice streams may deform the ice; these ice streams are detectable with their accompanying medial moraine, as seen during low-snow-year photography. Kinematic waves, in response to an accumulation perturbation, may cause minor surface bulging independent of base morphology. Interpretation of photographs taken over several years allows identification of these phenomena.

Catastrophic events can have long-term effects on a glacier's surface. The insulation of ice by rockfall results in the appearance of a raised underlying surface, a false indication of bedrock rise. An example of this is at Lost Creek Glacier on the South Sister (fig. 6), where existing maps, showing rockfall debris on the ice as bedrock, incorrectly identify the glacier as two separate ice fields.

The endpoints of each basal contour to be drawn are known at the ice-rock boundary. From basal contours well constrained by radar measurements, it was seen that the exposed valley walls would maintain their configuration for a distance subglacially. This seemed particularly true where the valley wall was very steep in the lower reaches of a well-developed valley glacier. The presence of morainal debris and stream sediment at the glacier terminus was considered in this interpretation.

Despite the use of radar measurements and photographs, data were limited for defining small-scale features in the basal contours. This necessitated smoothing of the contours and the drawing of small-scale features only where strictly warranted by the data.

The primary component of the error is this extrapolation of the local bedrock depths over a large subglacial area. Error made in the interpretation of bedrock topography by use of radar measurements and photographs was calculated at 16 percent. This was calculated by using independent interpretations of bedrock topography made by several glaciologists for South Cascade Glacier, which has a volume well known from previous intensive radar measurements.

#### ISOPACH MAPS AS INTERPRETIVE TOOLS

Isopach maps (pls. 2 and 5) are derived by the subtraction of altitudes between the surface and migrated



FIGURE 5.—Two views across Nisqually Glacier toward Wilson Glacier illustrating the use of aerial photographs in determining the location of bedrock. *A*, Glacier conditions during 1944 permitted exposure of a bedrock cliff in lower Wilson Glacier seen near the center of the photograph; *B*, The same area with bedrock submerged during 1980. (U.S. Geological Survey photographs by Fred Veatch on September 30, 1944, and by Carolyn Driedger on July 31, 1980.)

basal contours; they indicate areas of equal ice thickness.

Although these values are defined explicitly by the surface-basal maps, the isopach contour connecting them is subject to interpretation. Again, the simplest solution was chosen, with curvature and number of areas bounded minimized. All radar points were checked to assure that they were located in the correct thickness field.

Analyses of isopach maps reveal patterns in the ice thickness that indicate icefalls, rock ribs, and basins or irregularities in the surface-based maps. Therefore, the isopach map became an interactive tool in the process of refining the basal contour maps. For all measured glaciers, a graph that shows thickness as a function of area was prepared (figs. 11, 15, 19, 23).

## DETERMINATION OF VOLUMES

### MEASURED GLACIERS

Glacier volumes were found by determining the area between each set of bedrock and surface contours, a pair of which define a volume element (fig. 7). Areas were measured with a planimeter or a digitizer to within 3 percent accuracy and were completed for the length of the glacier. Volumes ( $V$ ) of each glacier were determined by using the volume-element areas in equation 3, where  $A_i$  is the area bounded by equally valued basal and surface contours at a given altitude and  $CI$  is the contour interval.



FIGURE 5.—Continued

$$V = \frac{CI \sum_{i=1}^n [A_i + (A_{i+1})]}{2} \quad (3)$$

The contour interval used was 200 feet on Mount Rainier and 100 feet on Mounts Hood and Shasta and the Three Sisters.

Glacier volumes were calculated by drainage area and altitude. Values for each drainage area, by mountain, are listed in tables 2 through 5. The percentage of the total ice and snow volume measured by radar varied for each mountain as follows: 62 on Mount Rainier, 83 on Mount Hood, 53 on the Three Sisters, and 19 percent on Mount Shasta.

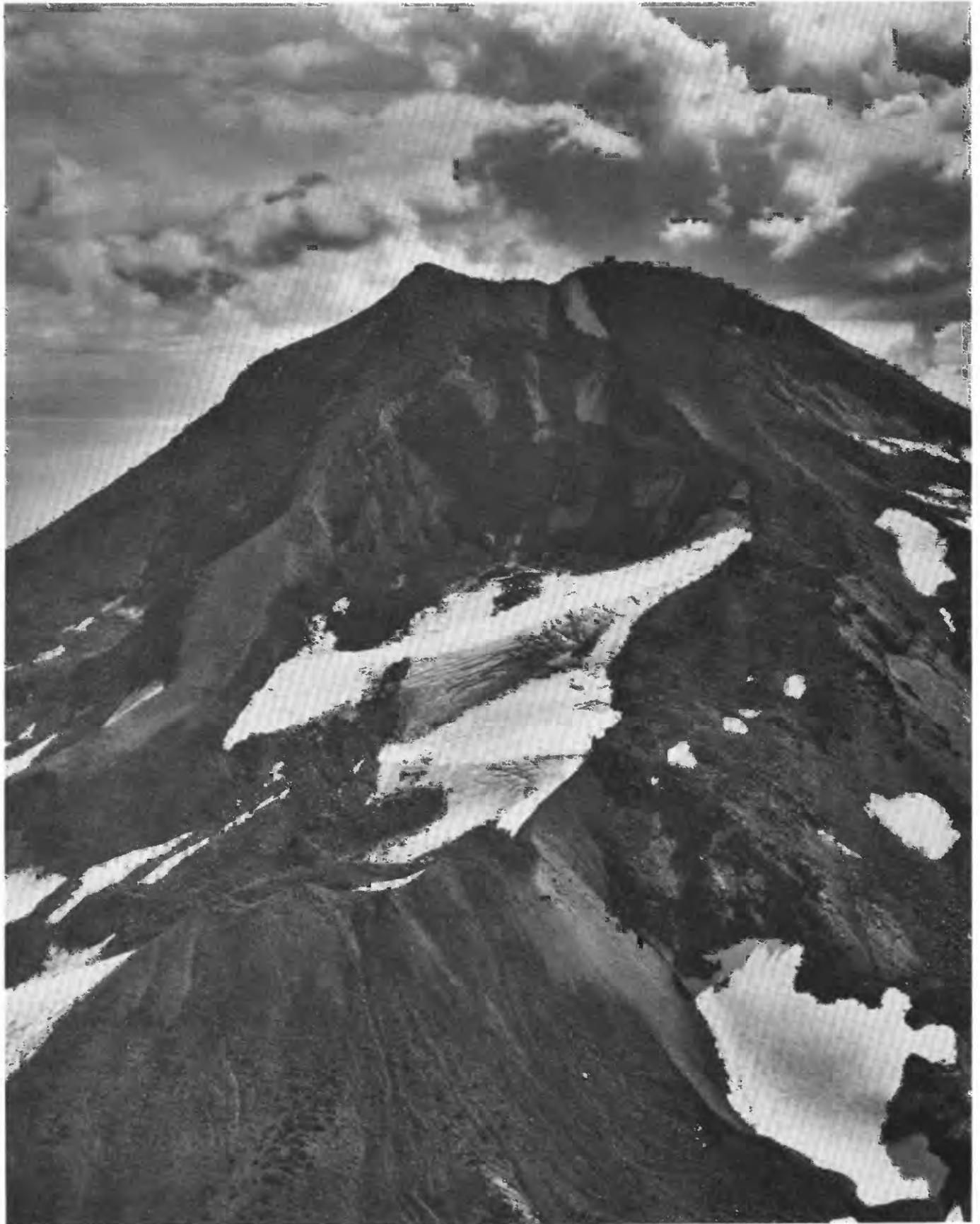
The error in calculating volume varied with each glacier, depending on the number of measurement points per glacier. Error in snow patch and ice

boundary corrections was estimated at 5 percent, and error from the original topographic maps was less than 5 percent. A conservative estimate for error in the volume of measured glaciers is  $\pm 20$  percent.

#### UNMEASURED GLACIERS AND SNOW PATCHES

Several different approaches have been made for estimating the volume or average thickness of unmeasured glaciers. For instance, Post and others (1971, p. 4) related average thickness to area size classes, using several measured glaciers for calibration. Kotliakov (1980) also incorporated the type of glacier in a similar scheme. Brückl (1973), Müller (1976, p. 12), Shih and others (1981, p. 194), Zhuravlev (1980), and Macheret and Zhuravlev (1982, p. 310) utilized an empirical relation of the form

$$\bar{h} = k_1 + k_2 A^m \quad (4)$$



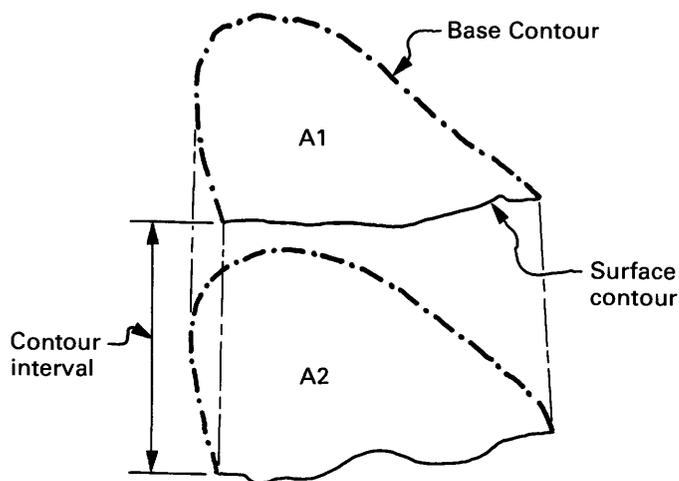


FIGURE 7.—Sketch showing one volume element, which, constructed over the length of the glacier, permits calculation of volume on the measured glaciers. Each element consists of two horizontal planes (A1 and A2) that are formed by surface and basal contours separated by the contour interval (Kennard, 1983).

where  $\bar{h}$  is the mean glacier thickness,  $k_1$ ,  $k_2$ , and  $m$  are coefficients derived from regression analysis,  $A$  is the glacier area, and  $m \sim 0.5$ .

Paterson (1970, p. 43) proposed that the shear stress on the bed be treated as a constant. For a simple, infinitely wide glacier with laminar flow, the shear stress on the bed  $\tau$  is

$$\tau = \rho gh \sin \alpha \quad (5)$$

where  $\rho$  is the ice density,  $g$  the acceleration of gravity,  $h$  the ice thickness, and  $\alpha$  the surface slope (Nye, 1952, p. 529). Thus, mean thickness can be calculated from the relation

$$\bar{h} = k_3/\alpha \quad (6)$$

where  $\alpha$  is the surface slope and  $k_3$  includes the assumed shear stress as well as ice density and geometric variables. However, none of these relations have been tested on glaciers of the type occurring on Cascade volcanoes.

Because glacier characteristics are related to latitude and climatic conditions, it was necessary to develop a volume estimation method for use in the Cascade Range. The volumes of unmeasured glaciers were estimated from statistical analysis of characteristics for all measured glaciers except the Whitney, which was examined during later study (Kennard, 1983). The

variables required for these volume estimations can be determined from topographic maps and aerial photographs.

Paterson's assumption of a constant basal shear stress, which is equivalent to the assumption that glacier flow can be treated by plasticity theory (Nye, 1951, p. 554), was tested by comparing shear stress (eq. 5) with other glacier characteristics. It was found that the larger glaciers had shear stress values in the expected range of  $1 < \tau < 2$  bars. However, the smaller glaciers had lower values of shear stress, ranging down almost to zero.

It would appear that some glaciers reach a critical basal shear stress, and for these glaciers, the flow is sufficiently fast to adjust the longitudinal profile to a dynamic equilibrium so that the product of thickness and surface slope is related to that stress. Other glaciers are too small to reach that critical shear stress, and their profiles are determined less by dynamic considerations than by local variations in snow drifting and melting. In an analysis of the measured glaciers (table 1), it was found that most glaciers having a length greater than 8,500 ft obtained a critical shear stress, and most glaciers having a length less than this

TABLE 1.—Table showing glacier lengths, mean glacier basal shear stresses calculated at 1,000-foot intervals, and assignment of a method giving the closest correlation with the glacier's measured volume, where A indicates a closer correlation with area and B indicates a closer correlation using a basal shear stress

Measured glacier	Correlation group	Basal shear stress, in bars	Map length of glacier, in thousands of feet
Emmons	B	1.6	23.5
Winthrop	B	1.4	26.5
Tahoma	B	1.4	24.3
Carbon	B	1.3	31.9
Nisqually	B	1.4	21.7
Eliot	B	1.4	13.1
Wilson	B	1.2	8.5
Coe	B	1.3	10.7
Whitney	A	0.5	9.2
Russell	A	0.7	7.8
Newton-Clark	A	0.5	6.7
Sandy	A	0.7	6.4
Collier	A	0.3	6.9
Prouty	A	0.5	5.1
Ladd	A	0.8	6.6
Reid	A	0.7	6.4
Zig zag	A	0.6	8.0
Hayden	A	0.6	4.3
Diller	A	0.5	3.9
White River	A	0.4	6.1
Lost Creek	A	0.4	4.7
Langille	A	0.6	4.8
Palmer	A	0.6	1.4
Coalman	A	0.6	1.6

FIGURE 6.—Rockfall partly concealing ice (left of center in the photograph), as seen here on Lost Creek Glacier in the Three Sisters, must be identified as such for the proper volume estimation. (U.S. Geological Survey photograph by Austin Post on September 10, 1980.)

did not. It was also found that an estimated basal shear stress  $\tau^*$  in pounds per square foot for the larger glaciers could be calculated by the empirical relation

$$\tau^* = 451.12 \left( \frac{\sum A_i}{\cos \alpha_i} \right)^{0.106} \quad (7)$$

where  $\sum A_i$  in feet squared is the sum of surface area at 1,000-foot altitude intervals. Noting that volume  $V = Ah$ , the estimated volume  $V^*$  in cubic feet can be calculated by using the estimated shear stress  $\tau^*$  according to

$$V^* = (\tau^*/\rho g) \sum (A_i/\cos \alpha_i \sin \alpha_i) \quad (8)$$

where area and slope were measured at 1,000-foot intervals and then summed.

Small glaciers, those that do not obtain the critical shear stress, were generally those less than 8,500 ft in length (Kennard, 1983). The empirical relationship is

$$V = 9.62A^{1.124} \quad (9)$$

where  $V$  equals volume in cubic feet of the total glacier and  $A$  equals total area in square feet. The Whitney Glacier on Mount Shasta, though measured by ice radar, is on the border of having a closer area correlation than a basal shear stress correlation. Its length is 9,200 ft but its shear stress is only 0.5 bars. Perhaps this may be explained by the presence of a substantial icefall around 11,800 ft that interrupts the normal glacier flow, essentially making it into two smaller glaciers. Some glaciers do not occupy discrete valley basins and their bedrock topography divides the glacier area into separate units. These should be treated separately for area determination and the results should be summed. Therefore, an experienced eye and much discretion are required in the application of and selection of a method for determining ice volume.

When the estimation methods were developed they were tested by application to glaciers with measured volumes. The standard deviations of errors of estimated and measured volumes were as follows: 5 percent for large glaciers (with volumes found by using equations 6 and 7), 16 percent for small glaciers (using equation 8), and 13 percent for the groups together. Together with a  $\pm 20$  percent uncertainty in finding measured glacier volumes, the error in using the estimation method is assumed to be about  $\pm 25$  percent.

## RESULTS FROM FOUR CASCADE VOLCANOES

### MOUNT RAINIER

Mount Rainier is west of the Cascade crest about 40 miles southeast of Tacoma, Wash. (fig. 8). The mountain, rising to 14,410 ft above sea level, dominates the landscape, and in fact, its geologic development has affected much of the surrounding local topography.

Water flows from the mountain in five major drainage basins. The Nisqually, Puyallup, Carbon, and White Rivers flow into Puget Sound, and the Cowlitz River flows into the Columbia River. Figure 9 indicates that the largest areas of snow and ice cover are in the watersheds of the Puyallup River (29 percent) and the White River (29 percent).

There are presently 23 major glaciers on Mount Rainier. These glaciers are some of the most accessible to the public in the nation. Descriptions and research on some, such as the Nisqually Glacier, date back to 1870 (Heliker and others, 1983, p. 3).

The five glacier systems measured on Mount Rainier are the Nisqually-Wilson, Tahoma, Carbon-Russell, Winthrop, and the Emmons. The volume of ice and snow on Mount Rainier is 156.2 billion ft<sup>3</sup>. Glacier and snow patch dimensions are listed by drainage area and by altitude in table 2. The maximum ice thickness measured on Mount Rainier is 705 ft, in the Carbon Glacier. With a volume of 25.1 billion ft<sup>3</sup>, the Carbon Glacier has the largest volume of the Rainier glaciers. At 3,500 ft in altitude, its terminus is the lowest of any in the conterminous States. The Nisqually Glacier, a glacier more commonly viewed by the public, has a surface area of 49.7 million ft<sup>2</sup>, whereas the Emmons has the largest surface area, at 120.2 million ft<sup>2</sup>. Figures 9 and 10 show ice areas by drainage as a function of altitude and ice volumes for radar-measured glaciers, respectively. Figure 11 shows measured ice areas at the indicated thickness intervals. Plate 1 is a map showing 1981 snow and ice boundaries and basal contours for the measured glaciers. Plate 2 shows the isopach maps derived from the surface-basal mapping of measured glaciers.

The interaction between glacial and volcanic activity predates the existing volcano form. Glacial till estimated to be as much as 600,000 years B.P. is covered by more recent intracanyon lava flows (Crandell and Miller, 1974, p. 17). More recently, the melting of ice and snow has in part been responsible for mudflows which extended to Enumclaw 6,000 years B.P. and to Orting about 500 years B.P. (Crandell and Mullineaux, 1981, p. 14). Figure 9 illustrates that 50 percent of snow and ice on the mountain is between altitudes of 6,000 and 9,000 feet; 30 percent is above 9,000 feet.



FIGURE 8.—Mount Rainier, Wash., as seen from the northwest, showing the Carbon (C), North Mowich (NM), Edmunds (E), and South Mowich (SM) Glaciers. Mowich Lake is in the foreground. (U.S. Geological Survey photograph by Robert Krimmel on August 17, 1981.)

Lahars are mudflows and debris flows of volcanic material derived from the slope of a volcano and sometimes mobilized with melting snow and ice. They occur

most often during periods of eruption, and, at Mount Rainier, they have occurred most frequently during historic times in the valleys of the White, Nisqually,

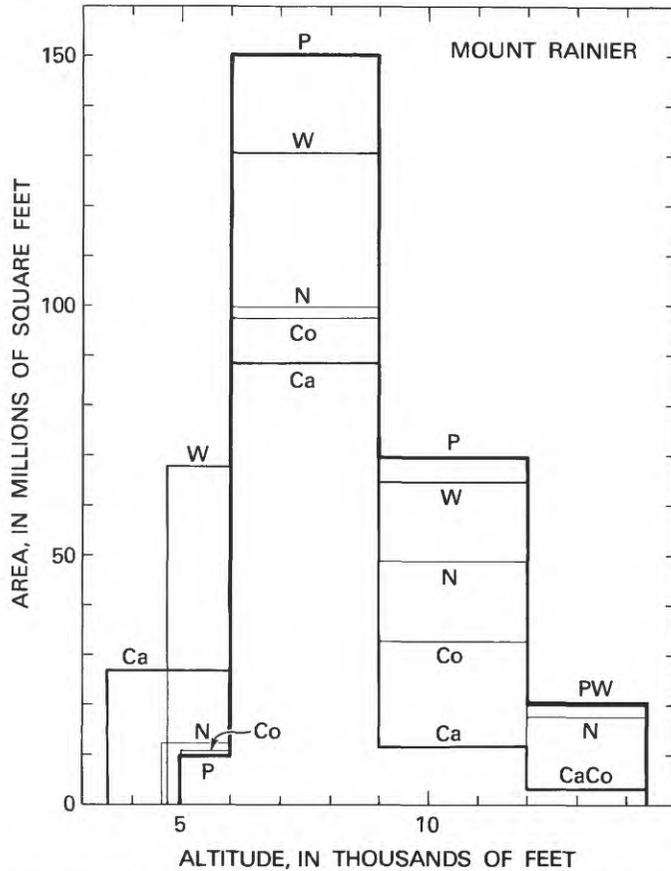


FIGURE 9.—Areas of ice and snow in Mount Rainier glacier drainage basins as a function of altitude. Drainage basins listed are as follows: Carbon (Ca), White River (W), Cowlitz (Co), Nisqually (N), and Puyallup (P).

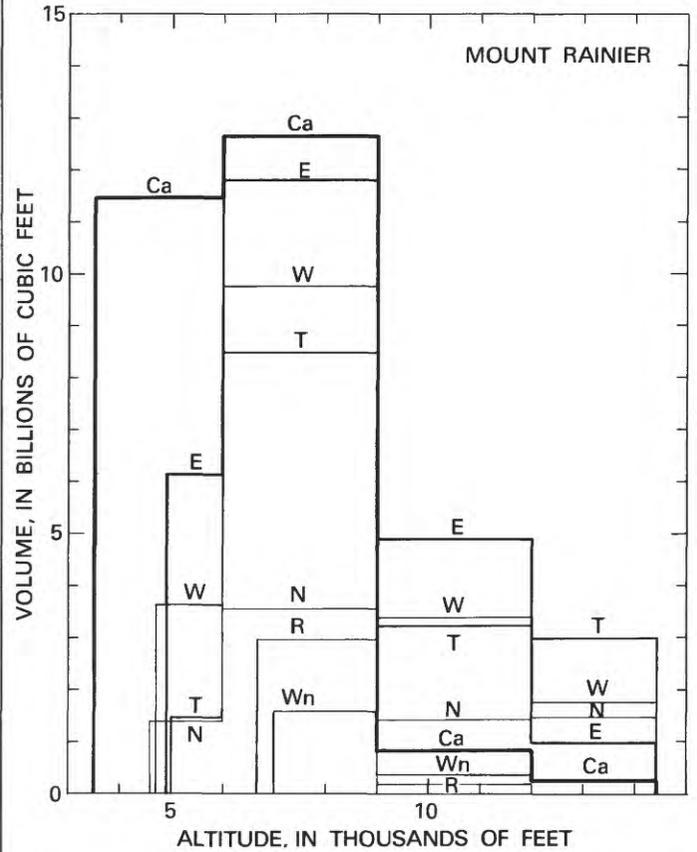


FIGURE 10.—Ice volume of measured Mount Rainier glaciers as a function of altitude. Glaciers listed are as follows: Carbon (Ca), Emmons (E), Nisqually (N), Tahoma (T), Winthrop (W), Wilson (Wn), and Russell (R).

and Mowich Rivers, and in Tahoma and Kautz Creeks. Lahars from Mount Rainier constitute the major threat to people and property during volcanic eruptions (Crandell, 1971, p. 69).

The summit depression contains two craters and is approximately the region above 12,000 ft. The region has an ice volume of 8.7 billion ft<sup>3</sup>. The tilt of the principal eastern crater toward the east indicates that this may be the first direction that meltwater in the center might flow. In such a situation, the Cowlitz, Ingraham, Emmons, and Winthrop Glaciers would be most affected; lahars and floods in the valleys of the Cowlitz and Whiter Rivers might result. The volumes of ice and snow are 20.2 billion ft<sup>3</sup> in the Cowlitz River and 47.2 billion ft<sup>3</sup> in the White River drainage areas. Further descriptions of Mount Rainier eruptive hazards are found in a publication by Crandell and Mullineaux (1981).

**MOUNT HOOD**

Mount Hood rises to 11,245 ft and is approximately 50 miles east of Portland, Oreg. (fig. 12). All the Mount Hood drainage systems (White, Zigzag, Sandy, and Hood Rivers) empty into the Columbia River. Figure 13 illustrates that 60 percent of the total area covered by snow and ice is in the Hood watershed. Figures 14 and 15 show ice volumes for radar-measured glaciers, and ice areas by drainage as a function of altitude.

Ice-volume measurements were made on all nine major glaciers of Mount Hood. The total volume of ice and snow on Mount Hood is 12.3 billion ft<sup>3</sup>. Glacier and snow-patch dimensions are listed by drainage area and by elevation in table 3. The Eliot Glacier has the largest volume, 3.2 billion ft<sup>3</sup>, and thickest measured ice, 361 ft. The Coe-Ladd Glacier system has the largest surface area, 23.1 million ft<sup>2</sup>.

TABLE 2.—Areas and volumes of glacier ice and snow on Mount Rainier

[Methods of determination: A, volume estimated by using area correlation; B, volume estimated with calculation of basal shear stress; M, glacier thickness measured by ice radar. Because total glacier areas are required in the application of both volume estimation methods, volumes are available by total glacier. Area measured in  $\text{ft}^2 (\times 10^6)$ ; volume measured in  $\text{ft}^3 (\times 10^9)$ . —in the area column means no ice or snow present for glacier at that elevation, and in the volume column it means volume by elevation not determined for that glacier]

Drainage Area	Glacier or Snow patch	Altitude Interval								Area total	Volume total	Method of determination
		3,000–6,000'		6,000–9,000'		9,000–12,000'		12,000–14,410'				
		Area	Volume	Area	Volume	Area	Volume	Area	Volume			
Cowlitz River	Snow patches	2.5	—	11	—	0.5	—	0.02	—	14.0	0.7	A
	Whitman	—	—	19.0	—	4.8	—	—	—	23.8	4.4	B
	Ingraham	3.56	—	18.8	—	16.6	—	3.6	—	42.6	7.0	B
	Cowlitz	4.5	—	21.3	—	11.0	—	—	—	36.8	6.0	B
	Paradise	—	—	10.9	—	—	—	—	—	10.9	.8	A
	Ohanapecosh	.3	—	17.0	—	—	—	—	—	17.3	1.3	A
Subtotal		10.9	—	98.0	—	32.9	—	3.6	—	145.4	20.2	
Nisqually River	Snow patches	—	—	7.4	—	.5	—	.4	—	8.3	.3	A
	Muir Snowfield	—	—	2.8	—	7.3	—	—	—	10.1	.7	A
	Nisqually	5.7	1.4	20	3.5	12.4	1.4	11.6	1.5	49.7	7.8	M
	Wilson	—	—	10.8	1.6	4.7	.3	—	—	15.5	1.9	M
	Kautz	—	—	6.4	—	5.7	—	.3	—	12.4	1.3	A
	Success	—	—	3.6	—	3.8	—	—	—	7.4	.5	A
	Van Trump	—	—	5.6	—	1.1	—	—	—	6.7	.5	A
	Pyramid	—	—	5.6	—	.2	—	—	—	5.8	.4	A
	S. Tahoma	2.6	—	19.5	—	8.1	—	.2	—	30.4	4.6	B
Tahoma	3.6	.4	18.2	2.9	5.0	.5	5.3	.5	32.1	4.3	M	
Subtotal		11.9		99.9		48.8		17.8		178.4	22.3	
Puyallup River	Snow patches	—	—	9.7	—	.2	—	—	—	9.9	.4	A
	Tahoma	5.1	1.0	23.0	5.6	18.8	2.7	13.96	2.5	60.8	11.8	M
	N. Mowich	3.0	—	48.3	—	13.7	—	1.4	—	66.4	9.5	A
	Liberty Cap	—	—	—	—	.4	—	1.3	—	1.7	.1	A
	Flett	—	—	3.2	—	—	—	—	—	3.2	.2	A
	Edmonds	—	—	11.3	—	3.7	—	—	—	15.0	1.1	A
	S. Mowich	.8	—	16.4	—	19.5	—	1.7	—	38.4	4.5	B,A
	Puyallup	1.1	—	38.2	—	13.6	—	1.9	—	54.8	10.2	B
Subtotal		10.0		150.1		69.9		20.2		250.2	37.8	
Carbon River	Snow patches	.3	—	9.2	—	—	—	—	—	9.5	.5	A
	Carbon	26.6	11.4	46.1	12.6	9.4	.8	3.1	.2	85.2	25.1	M
	Russell	—	—	33.2	3.0	2.3	.1	—	—	35.5	3.1	M
Subtotal		26.9		88.5		11.7		3.1		130.2	28.7	
White River	Snow patches	.9	—	16.6	—	1.1	—	—	—	18.6	1.0	A
	Winthrop	18.5	3.6	44.3	9.7	23.7	3.4	11.6	1.8	98.1	18.5	M
	Emmons	16.4	6.1	55.7	11.8	39.4	4.9	8.7	.9	120.2	23.8	M
	Inter	—	—	7.4	—	1.0	—	—	—	8.4	.6	A
	Fryingpan	32.4	—	2.8	—	—	—	—	—	35.2	2.9	A
	Sarvent	.1	—	6.1	—	—	—	—	—	6.2	.4	A
Subtotal		68.3		132.9		65.2		20.3		286.7	47.2	
Total		128.0		569.4		228.5		65.0		990.9	156.2	

The ice and snow boundaries on Mount Hood and basal contours for the measured glaciers in 1981 are shown on plate 3. The isopach maps derived from the surface-basal contours are shown on plate 5.

Mount Hood's composite cone was built during late Pleistocene time (Wise, 1969, p. 969). Its earliest known major eruptive period after the glacial maximum occurred 12,000 to 15,000 years B.P., which, along with two other major eruptive periods (1,500–1,800 and 200–300 years B.P.) produced much of the mountain visible today (Crandell, 1980, p. 1). Much of the topography on the lower slopes of Mount Hood is the result of mudflows and pyroclastic flows, which were formed during the Polallie eruptive period of

12,000 to 15,000 years B.P. and may have been aided by eruption-related icemelt. The absence of these deposits in some valleys indicates the extent of former glaciers (Crandell, 1980, p.11).

As on Mount Rainier, the river valleys radiating from Mount Hood contain valuable timber and recreational property. The geologically recent eruptive history and hazards of Mount Hood were more comprehensively described in Crandell (1980).

At Mount Hood flooding and lahars are the principal eruptive hazard to these resources. Crandell (1980, p. 56) stated that they represent a hazard in the valleys—up to several tens of feet high on the valley walls and higher where the valley is constricted. Interpreta-

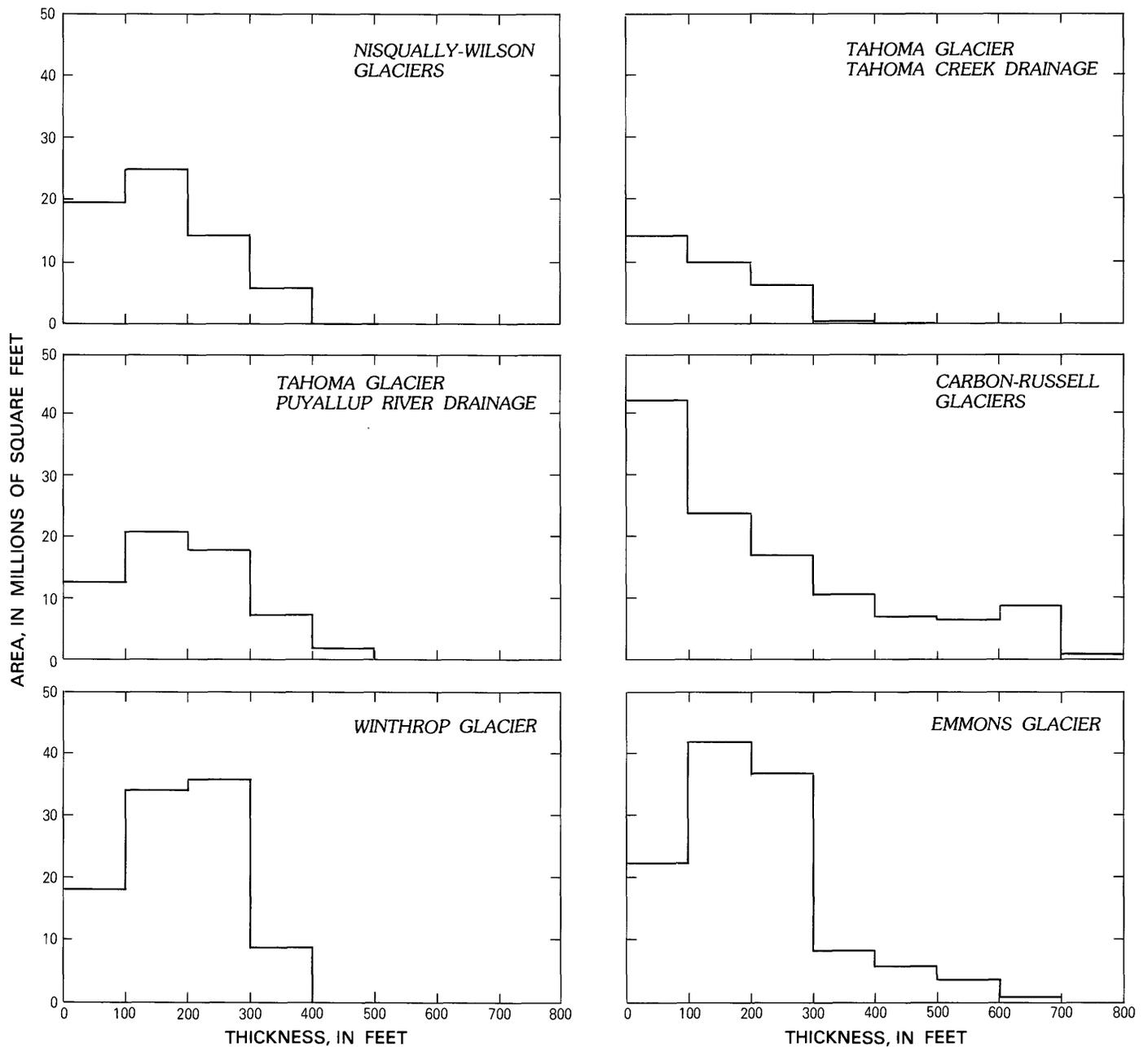


FIGURE 11.—Areas of selected thickness intervals of radar-measured glaciers of Mount Rainier. Values are derived from isopach maps.

tions of the hazard map developed by Crandell indicate that a dome-building eruption in the present Crater Rock region might deposit debris on the White River, Palmer, Zigzag, and Reid Glaciers and affect about 2 billion  $\text{ft}^3$  of ice and snow. The volume of ice above 10,000 ft in the vicinity of Crater Rock is about 47 million  $\text{ft}^3$ . About 80 percent of the total area of snow and ice cover is above 7,000 feet in altitude.

An eruption outside the debris fan region, but near the summit, might cause eruptive deposits on the remainder of the Mount Hood glaciers, which have an ice and snow volume of 10.5 million  $\text{ft}^3$ .

#### THREE SISTERS

In this report, the name Three Sisters collectively refers to the North Sister, Middle Sister, and South

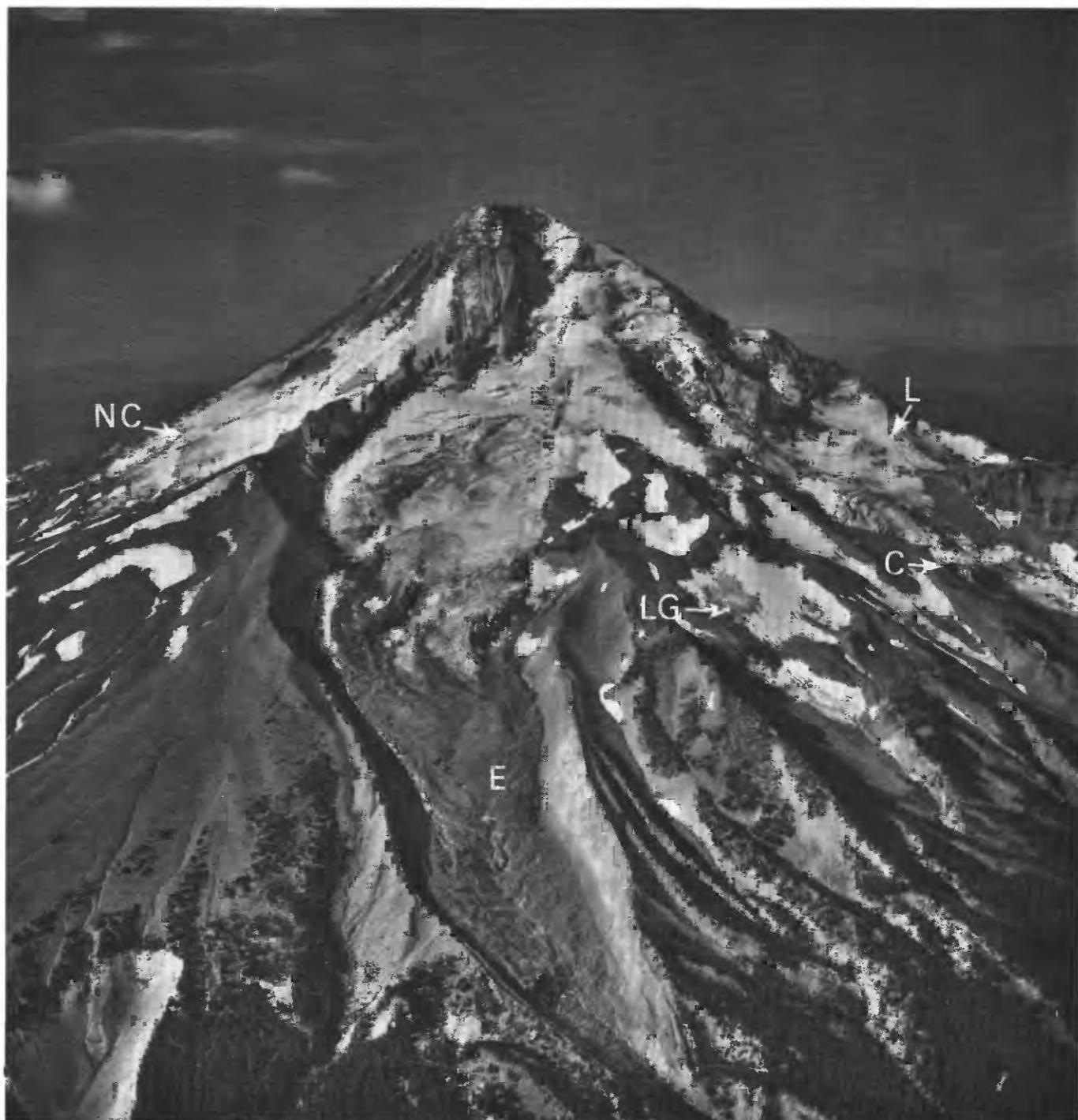


FIGURE 12.—Mount Hood, Oreg., as seen from the east, showing Newton-Clark (NC), Eliot (E), Langille (LG), Coe (C), and Ladd (L) Glaciers. (U.S. Geological Survey photograph by Austin Post on September 10, 1980.)

Sister, three volcanic cones located in an extensive volcanic region about 30 miles west of Bend, Oreg. The Three Sisters have a total ice and snow volume of 5.6 billion ft<sup>3</sup>, as seen in table 4.

Four major streams drain the Three Sisters. Separation Creek and White Branch drain the west sides of the mountains and empty into the McKenzie River. Squaw Creek drains most of the Three Sisters' east side

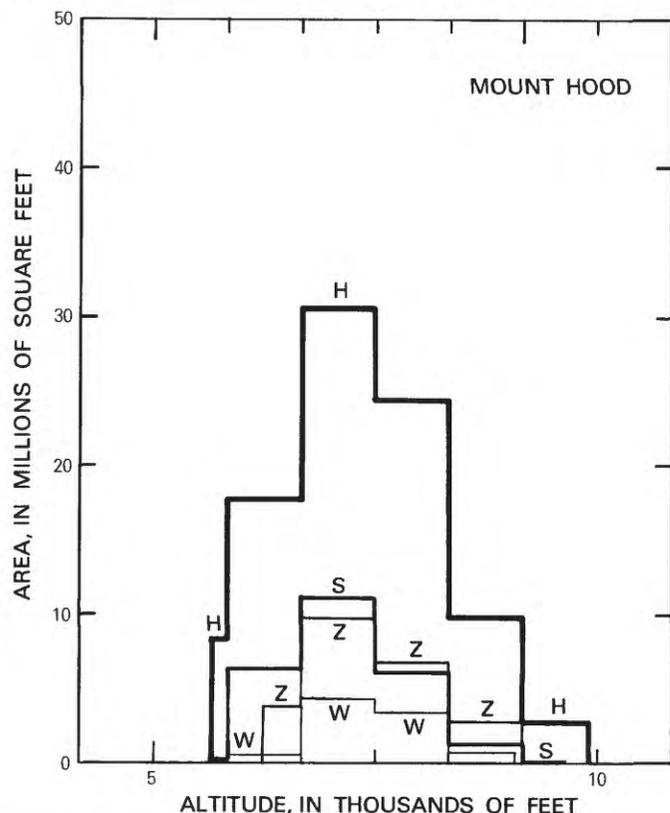


FIGURE 13.—Areas of ice and snow in Mount Hood glacier drainage basins as a function of altitude. Drainage basins listed are as follows: Hood River (H), Sandy River (S), White River (W), and Zigzag (Z).

and empties into the Deschutes River, after flowing through the town of Sisters. Forty-three percent of the total surface area of snow and ice is in the Squaw Creek watershed. Fall Creek drains the southeastern part of South Sister, where flank eruptions have occurred in postglacial time. Five miles from South Sister it empties into Sparks Lake, which has no surface outlet.

Radar measurements were made on the five major glaciers on the Three Sisters: Hayden, Diller, Collier, Prouty, and Lost Creek Glaciers. As seen in table 4, Collier Glacier (in the Squaw Creek and White Branch drainage areas) is the largest, with a surface area of 11.8 million ft<sup>2</sup>, a volume of 0.7 million ft<sup>3</sup>, and the greatest ice thickness at 300 ft. Plate 4 displays basal contours and plate 5 displays isopachs for the measured glaciers.

Volcanism in the Three Sisters region is varied in origin and type, with eruptions predating and postdating the eruption of Mount Mazama about 6,800 years B.P. (Wozniak and Taylor, 1981, p. 61). The larger relief features consist of three cones more than 10,000 ft in altitude—North, Middle, and South Sisters, which erupted in pre-Holocene time—and the smaller cones of

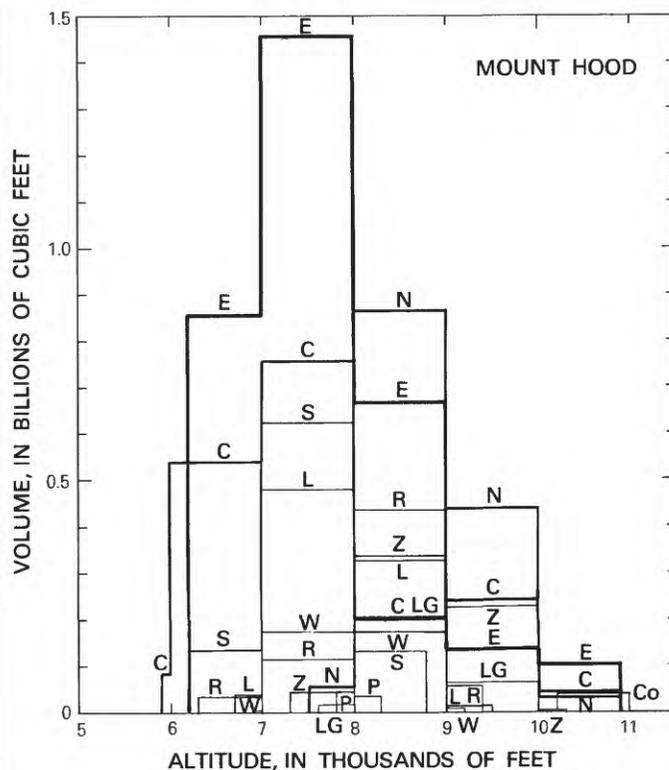


FIGURE 14.—Ice volume of measured Mount Hood glaciers as a function of altitude. Glaciers listed are as follows: Coe (C), Coalman (Co), Eliot (E), Ladd (L), Langille (LG), Newton-Clark (N), Palmer (P), Reid (R), Sandy (S), White River (W), and Zigzag (Z).

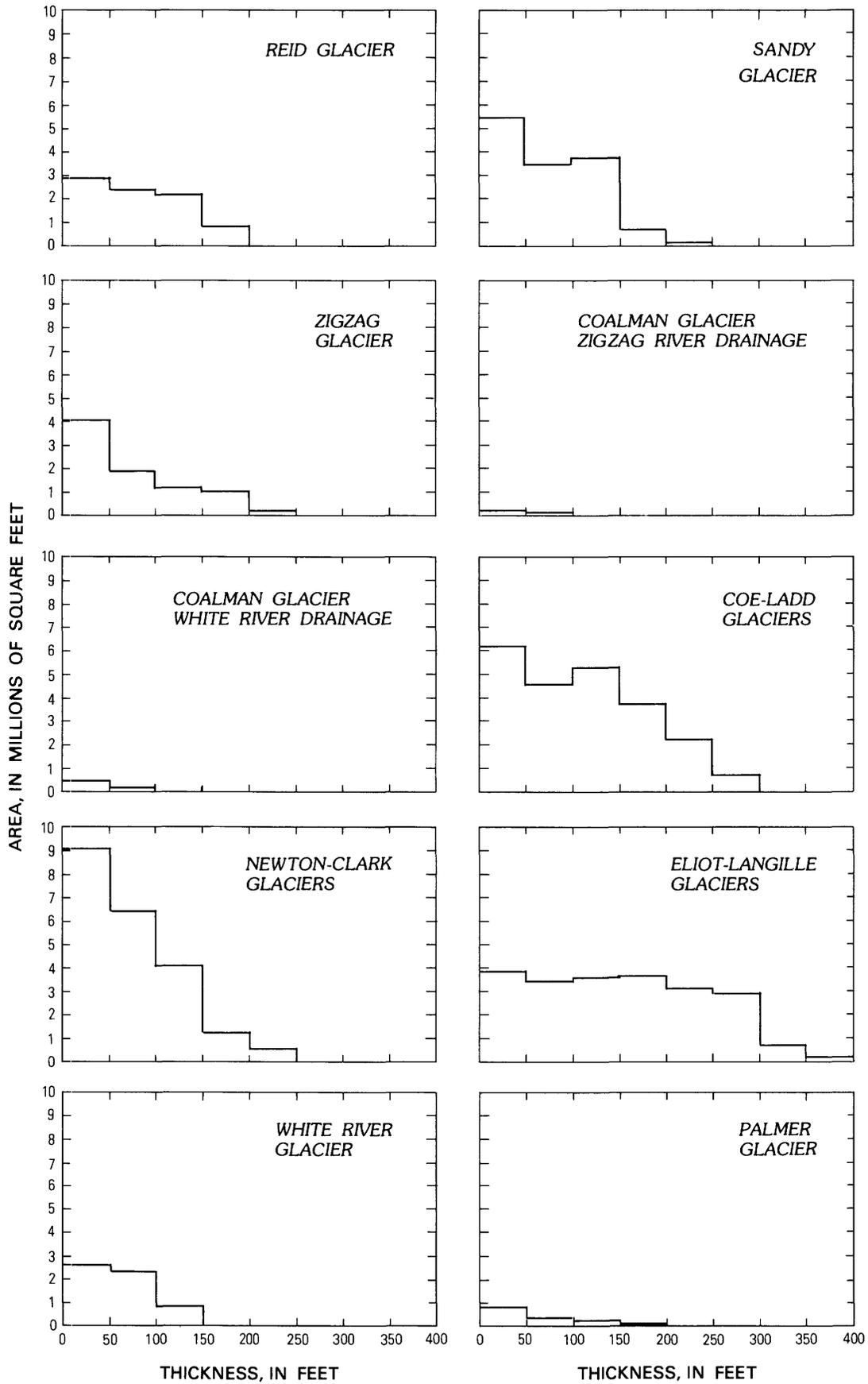
Broken Top (pre-Holocene) and Bachelor Butte (Pleistocene to Holocene time, fig. 16). More recently, basalt has flowed over extensive regions north and south of the Three Sisters. A rhyodacitic flank eruption on the south side of South Sister is the most recent activity on the Sisters cones.

The lack of widespread mudflow and pyroclastic deposits from the most recent summit eruptions on South Sister indicates that these eruptions may have occurred during late Wisconsin time when an extensive ice cover surrounded the cone. Though no direct geologic evidence exists to indicate large-scale glacier melting during past eruptions, there is evidence that some late Holocene flank eruptions were accompanied by small lahars, which were probably aided by rapid snowmelt (W. E. Scott, U.S. Geological Survey, written commun., May 18, 1983).

Regional eruptive patterns during the Holocene indicate that future rhyodacitic eruptions accompanied by small pyroclastic flows and tephra could occur on the south flank of South Sister in the presence of seasonal snow cover and glacier ice. Figure 17 illustrates that

FIGURE 15.—Areas of ice for each thickness interval of radar-measured glaciers. Values are derived from isopach maps of Mount Hood (Kennard, 1983). ▶

RESULTS FROM FOUR CASCADE VOLCANOES



## ICE VOLUMES ON CASCADE VOLCANOES

TABLE 3.—Areas and volumes of glacier ice and snow on Mount Hood

[Methods of determination: A, volume estimated by using area correlation; M, glacier thickness measured by ice radar. Because total glacier areas are required in the application of the volume estimation method, volumes are available by total glacier. Area measured in ft<sup>2</sup> (×10<sup>6</sup>); volume measured in ft<sup>3</sup> (×10<sup>9</sup>). — in the area column means no ice or snow present for glaciers at that elevation, and in the volume column it means volume by elevation not determined for that glacier]

Drainage area	Glacier or snow patch	Altitude Interval												Area total	Volume total	Method of determination		
		5,000–6,000'		6,000–7,000'		7,000–8,000'		8,000–9,000'		9,000–10,000'		10,000–11,000'					11,000–11,245'	
		Area	Volume	Area	Volume	Area	Volume	Area	Volume	Area	Volume	Area	Volume	Area	Volume			
White River	Snow patches	—	—	0.5	—	1.2	—	0.8	—	0.4	—	—	—	—	—	2.9	0.2	A
	Coalman	—	—	—	—	—	—	—	—	—	—	.6	.03	—	—	.6	.03	M
	White River	—	—	.01	.0008	3.2	.2	2.3	.19	.3	.008	—	—	—	—	5.8	.3	M
	Subtotal	—	—	.5	—	4.4	—	3.1	—	.7	—	.6	—	—	—	9.3	.5	
Hood River	Snow patches	.5	—	8.3	—	9.9	—	.6	—	—	—	—	—	.1	—	19.4	1.0	A
	Newton-Clark	—	—	—	—	2.1	.05	12.3	.9	5.7	.4	1.3	.03	—	—	21.4	1.4	M
	Coe	.3	.09	3.7	.5	5.0	.8	2.0	.2	1.7	.2	.7	.04	—	—	13.4	1.9	M
	Ladd	—	—	1.0	.04	5.9	.5	2.5	.3	.3	.01	—	—	—	—	9.7	.9	M
	Eliot	—	—	4.6	.9	7.2	1.4	4.1	.7	1.3	.1	.9	.1	—	—	18.1	3.2	M
	Langille	—	—	—	—	.4	.02	2.9	.2	1.0	.06	—	—	—	—	4.3	.3	M
	Subtotal	.8	—	17.6	—	30.5	—	24.4	—	10.0	—	2.9	—	.1	—	86.3	8.7	
Zigzag River	Snow patches	—	—	3.9	—	7.8	—	1.5	—	.5	—	—	—	.2	—	13.9	.7	A
	Zigzag	—	—	—	—	1.3	.04	4.5	.3	2.4	.2	.1	.005	—	—	8.3	.6	M
	Palmer	—	—	—	—	.6	.04	.8	.03	—	—	—	—	—	—	1.4	.07	M
	Coalman	—	—	—	—	—	—	—	—	—	—	.3	.01	—	—	.3	.01	M
	Subtotal	—	—	3.9	—	9.7	—	6.8	—	2.9	—	.4	—	.2	—	23.9	1.4	
Sandy River	Snow patches	.2	—	2.3	—	.8	—	.4	—	.3	—	.6	—	.1	—	4.7	.2	A
	Sandy	—	—	3.1	.1	8.0	.6	1.7	.1	—	—	—	—	—	—	12.8	.8	M
	Reid	—	—	.9	.03	2.2	.1	4.0	.4	1.0	.06	—	—	—	—	8.1	.6	M
	Subtotal	.2	—	6.3	—	11.0	—	6.1	—	1.3	—	.6	—	.1	—	25.6	1.7	
	Total	1.0	—	28.3	—	55.6	—	40.4	—	14.9	—	4.5	—	.4	—	145.1	12.3	

TABLE 4.—Areas and volumes of glacier ice and snow on Three Sisters

[Methods of determination: A, volume estimated by using area correlation; M, glacier thickness measured by ice radar. Because total glacier areas are required in the application of the volume estimation method, volumes are available by total glacier. Area measured in ft<sup>2</sup> (×10<sup>6</sup>); volume measured in ft<sup>3</sup> (×10<sup>9</sup>). — in the area column means no ice or snow present for glaciers at that elevation, and in the volume column it means volume by elevation not determined for that glacier]

Drainage area	Glacier or snow patch	Altitude Interval										Area total	Volume total	Method of determination
		6,000–7,000'		7,000–8,000'		8,000–9,000'		9,000–10,000'		13,000–14,162'				
		Area	Volume	Area	Volume	Area	Volume	Area	Volume	Area	Volume			
Squaw Creek	Snow patches	0.1	—	4.7	—	1.5	—	0.1	—	—	—	6.4	0.3	A
	Linn	—	—	—	—	.6	—	—	—	—	—	.6	.03	A
	Villard	—	—	—	—	.1	—	.4	—	—	—	.5	.02	A
	Thayer	—	—	1.1	—	.6	—	—	—	—	—	1.7	.1	A
	Hayden	—	—	.7	.07	6.8	.6	.3	.009	—	—	7.8	.6	M
	Diller	—	—	2.9	.2	4.2	.3	—	—	—	—	7.1	.5	M
	Carver	—	—	1.9	—	1.6	—	—	—	—	—	3.5	.2	A
	Prouty	—	—	.3	.03	7.9	.4	2.3	.1	.004	.001	10.5	.7	M
	Collier	—	—	—	—	.4	.004	—	—	—	—	.4	.004	M
		Subtotal	.1	—	11.6	—	23.7	—	3.1	—	.004	—	38.5	2.5
Fall Creek	Snow patches	—	—	1.3	—	1.4	—	.4	—	—	—	3.1	.1	A
	Lewis	—	—	—	—	1.6	—	2.6	—	—	—	4.2	.3	A
	Subtotal	—	—	1.3	—	3.0	—	3.0	—	—	—	7.3	.4	
Separation Creek	Snow patches	—	—	.6	—	1.5	—	.6	—	—	—	2.7	.1	A
	Clark	—	—	—	—	3.0	—	—	—	—	—	3.0	.2	A
	Lost Creek	—	—	1.5	.05	4.1	.4	.2	.003	—	—	5.8	.4	M
	Crater	—	—	—	—	—	—	—	—	1.1	.07	1.1	.06	M
	Eugene	—	—	—	—	—	—	1.0	.006	—	—	1.0	.05	A
	Skinner	—	—	1.7	—	1.4	—	—	—	—	—	3.1	.2	A
	Irving	—	—	3.4	—	.6	—	.1	—	—	—	4.1	.3	A
	Subtotal	—	—	7.2	—	10.6	—	1.9	—	1.1	—	20.8	1.3	
White Branch	Snow patches	—	—	3.1	—	1.9	—	.3	—	—	—	5.3	.3	A
	Renfrew	—	—	.3	—	5.2	—	.5	—	—	—	6	.4	A
	Collier	—	—	3.1	.2	7.9	.5	.4	.005	—	—	11.4	.7	M
	Subtotal	—	—	6.5	—	15.0	—	1.2	—	—	—	22.7	1.4	
	Total	.1	—	26.6	—	52.3	—	9.2	—	1.1	—	89.3	5.6	



FIGURE 16.—South, Middle, and North Sisters and the slope of Broken Top, Oreg., as seen (left to right) from the southeast. Lewis (L) and Prouty (P) Glaciers are visible on slopes of South Sister. Diller (D) and Hayden (H) Glaciers are visible on right flank of Middle Sister. Most recently erupted lava of 2,000 to 3,000 years ago is visible on the south flank of South Sister. (U.S. Geological Survey photograph by Robert Krimmel on August 18, 1981.)

47 percent of the area covered by snow and ice is on the South Sister. In this drainage basin are the Prouty and Lewis Glaciers, with a total volume of 0.8 billion ft<sup>3</sup>. Basaltic eruptions north and south of the Sisters could pose an additional hazard if erupted onto thick snowpack. Figures 18 and 19 show ice volumes for radar-

measured glaciers, and ice areas by drainage as a function of altitude.

More information on the geology of the Three Sisters volcanic region is available in the recent report by Taylor (1981).

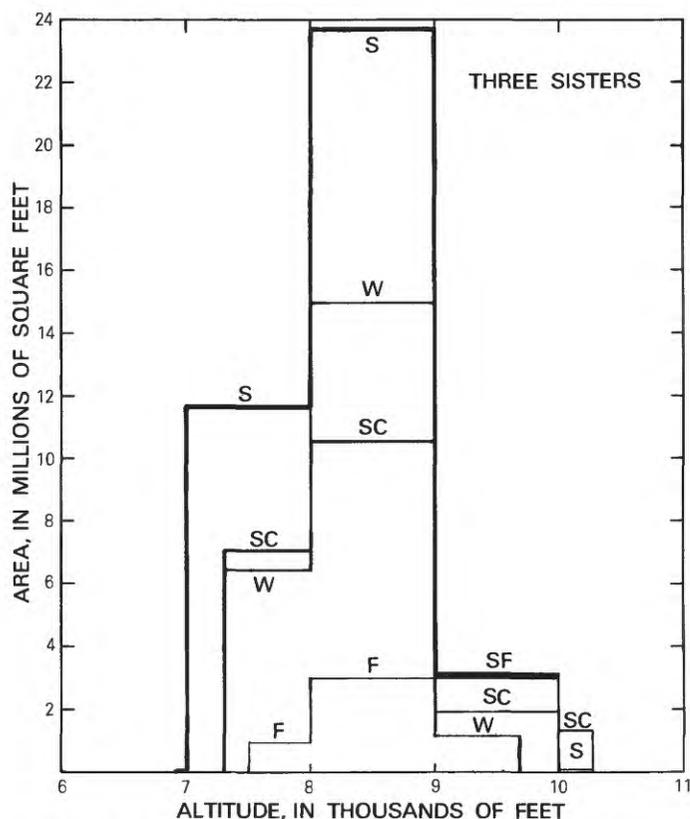


FIGURE 17.—Areas of ice and snow in the Three Sisters drainage basins as a function of altitude. Drainage basins listed are as follows: Fall Creek (F), Separation Creek (S), Squaw Creek (SC), and White Branch (W).

#### MOUNT SHASTA

Mount Shasta (fig. 20), with an ice volume of 4.7 billion  $\text{ft}^3$ , is about 40 miles south of the Oregon-California border.

Snowmelt and glacial meltwater flow from Mount Shasta in four major drainage systems that are shown on plate 6. Several intermittent creeks that are tributary to the Shasta River and to the south branch of the Klamath River drain Mount Shasta, including its most developed glacier, Whitney. Thirty-nine percent of the area covered by snow and ice is in the Klamath River watershed. The massive volcano is drained on the northeast side by several intermittent creeks, which enter a small closed depression southeast of Whaleback Mountain. Numerous creeks drain the mountain's southeast side and enter the McCloud River, which flows south to the Sacramento River. The southwest sides of Mount Shasta and the satellite cone of Shastina are in the Sacramento River drainage area, where several intermittent streams drain the region before disappearing into the porous volcanic rocks above the town of Mount Shasta.

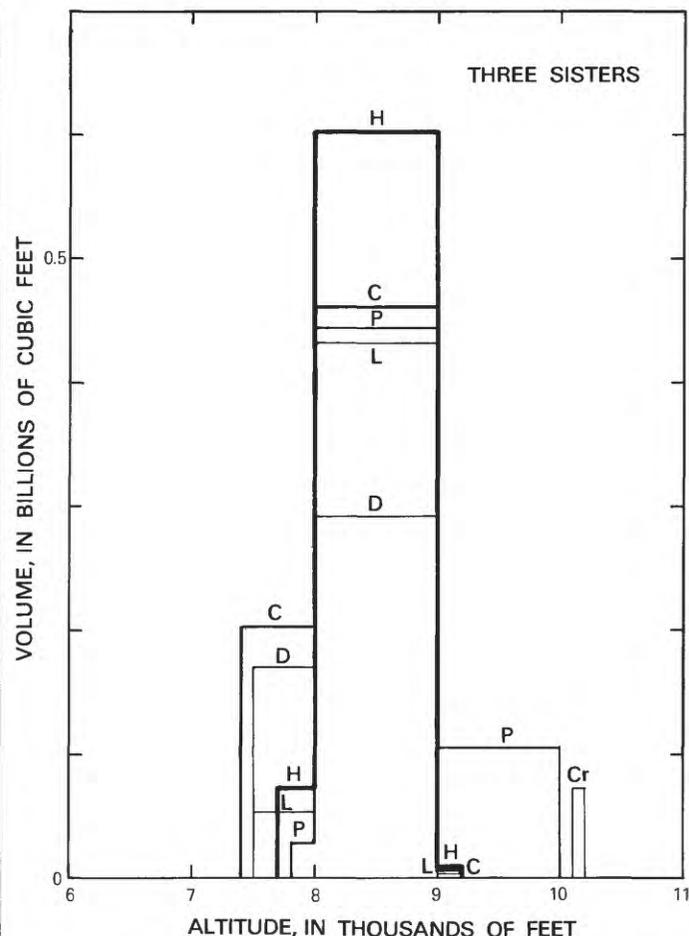


FIGURE 18.—Ice volumes of measured glaciers of the Three Sisters volcanoes as a function of altitude. Glaciers listed are as follows: Collier on North Sister (C), Crater on South Sister (Cr), Diller on North Sister (D), Hayden on North Sister (H), Lost Creek on South Sister (L), and Prouty on South Sister (P).

Though the main lobe of the Hotlum Glacier is the largest in area (19.4 million  $\text{ft}^2$ ) and in volume (1.3 billion  $\text{ft}^3$ ), the thickest ice measured on Mount Shasta is the 126 ft recorded on the Whitney Glacier. Whitney Glacier is the only glacier on Mount Shasta measured successfully by ice radar, having an area of 14 million  $\text{ft}^2$  and a volume of 0.9 billion  $\text{ft}^3$  (see table 5). Isopachs for Whitney Glacier are seen in plate 6.

Mount Shasta is a compound stratovolcano composed of overlapping deposits erupted during a period of several hundred thousand years. Past eruptive events have included dome building, lava flows, pyroclastic flows, mudflows, and some small volume eruptions of tephra. Similar future eruptions could occur near the present summit or could form new vents such as Shastina and Black Butte, both west of Mount Shasta (Miller, 1980, p. 28).

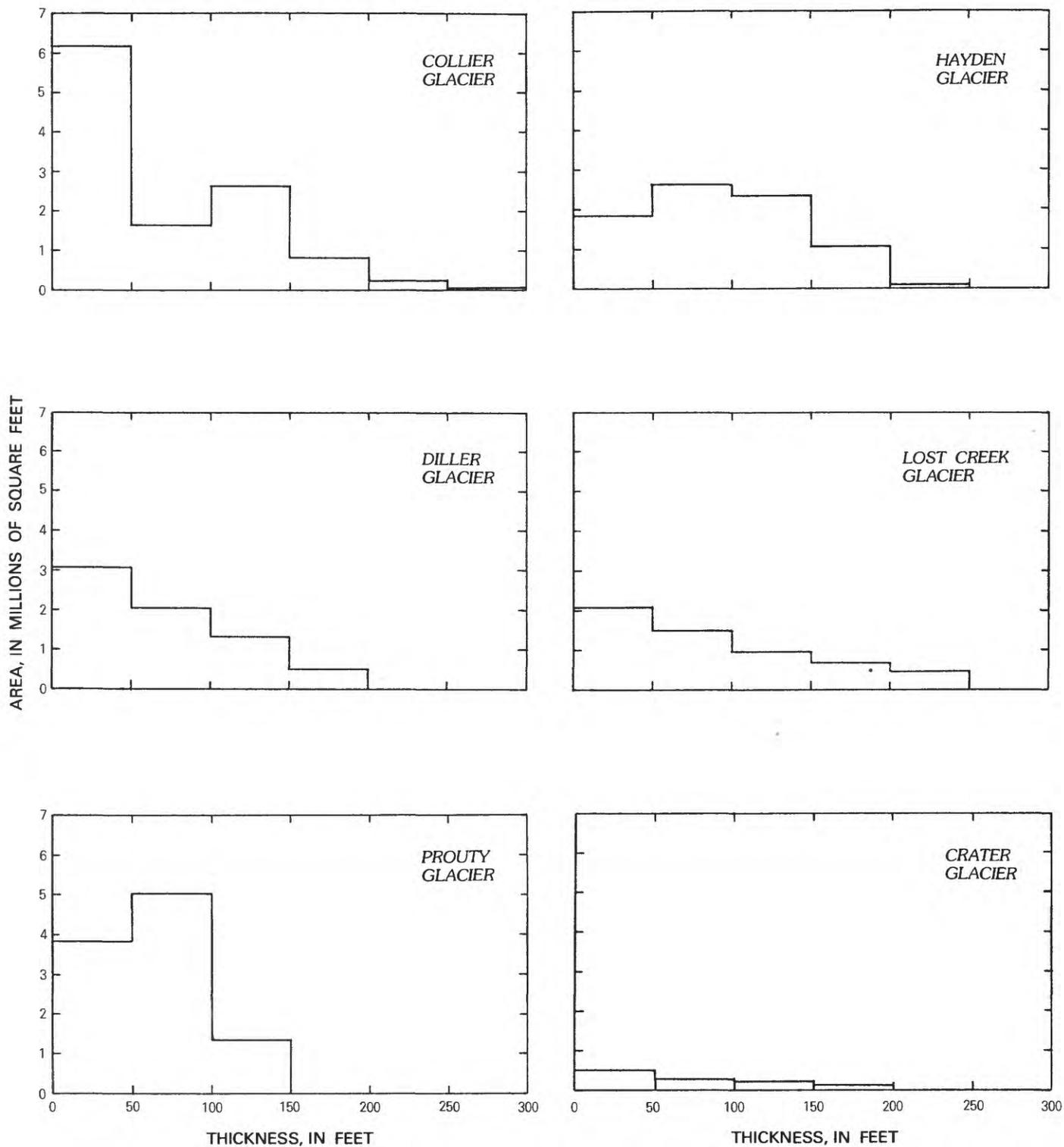


FIGURE 19.—Areas of ice for selected thickness intervals on radar-measured glaciers of the Three Sisters volcanoes. Values are derived from isopach maps.

Unlike the valleys on Mount Rainier, those on Mount Shasta are not of great length and thus allow mudflows, lava flows, and pyroclastics to form deposits

around the flanks of the mountain rather than many miles distant (Miller, 1980, p. 31).



FIGURE 20.—Mount Shasta, Calif., as seen from the northwest. The Whitney Glacier (W) flows between Mount Shasta (left) and Shastina (right). The Bolam (B) and Hotlum (H) Glaciers are on the left flank of Mount Shasta. (U.S. Geological Survey photograph by Robert Krimmel on August 19, 1981.)

Lava generally flows in existing valleys and, because of its viscous nature, is limited in areal extent. In Holocene time, lava was erupted most often near the summit and less often from the lower flanks of Mount Shasta. Past lava flows have been thick and blocky and have rarely extended more than 5 miles from their source, which is in the presence of some snow and ice.

Pyroclastic flows, with the potential for covering large areas of ice and snow, have been frequent in the last 10,000 years and have flowed as far as 12 miles from their source (Miller, 1980, p. 14). Though their extent depends upon the composition of gas in the eruption, it is probable they will flow over snow and ice.

TABLE 5.—Areas and volumes of glacier ice and snow on Mount Shasta

[Methods of determination: A, volume estimated by using area correlation; M, glacier thickness measured by ice radar. Because total glacier areas are required in the application of the volume estimation method, volumes are available by total glacier. Area measured in  $\text{ft}^2 (\times 10^6)$ ; volume measured in  $\text{ft}^3 (\times 10^9)$ . — in the area column means no ice or snow present for glaciers at that elevation, and in the volume column it means volume by elevation not determined for that glacier]

Drainage area	Glacier or snow patch	Altitude Interval										Area total	Volume total	Method of determination
		9,000–10,000'		10,000–11,000'		11,000–12,000'		12,000–13,000'		13,000–14,162'				
		Area	Volume	Area	Volume	Area	Volume	Area	Volume	Area	Volume			
Valley basin	Snow patches	—	—	0.7	—	—	—	—	—	—	—	0.7	0.05	A
	Hotlum #1	—	—	4.0	—	6.2	—	3.4	—	.8	—	14.4	1.0	A
	Subtotal	—	—	4.7	—	6.2	—	3.4	—	.8	—	15.1	1.1	
Klamath	Snow patches	.7	—	1.9	—	1.3	—	—	—	—	—	3.9	.2	A
	Bolam	.1	—	3.5	—	5.0	—	2.3	—	.5	—	11.4	.8	A
	Whitney	.2	1.4	5.0	292.0	2.7	188.97	2.9	276.8	3.0	158.8	13.8	.9	M
	Subtotal	1.0	—	10.4	—	9.0	—	5.2	—	3.5	—	29.1	1.9	
Sacramento	Snow patches	—	—	1.3	—	3.5	—	1.5	—	.5	—	6.8	.3	A
	Subtotal	—	1.3	—	3.5	—	1.5	—	.5	—	6.8	.3		
McCloud	Snow patches	.4	—	.8	—	—	—	.2	—	—	—	1.4	.07	A
	Hotlum #2	—	—	1.3	—	2.4	—	1.1	—	.2	—	5.0	.3	A
	Wintun	1.0	—	2.8	—	4.7	—	3.1	—	1.6	—	13.2	.9	A
	Konwakiton	—	—	—	—	.4	—	1.4	—	1.4	—	3.2	.2	A
	Subtotal	1.4	—	4.9	—	7.5	—	5.8	—	3.2	—	22.8	1.4	
	Total	2.4	—	21.3	—	26.2	—	15.9	—	8.0	—	73.8	4.7	

Floods are common events during volcanic eruptions because of snowmelt and icemelt. Those originating on volcanoes may be more damaging than floods elsewhere due to their high sediment concentration. Mudflows, many unrelated to eruptions, have traveled more than 16 miles from the summit of Mount Shasta in the valleys of Mud, Ash, Whitney, and Bolam Creeks and in the valleys of the McCloud and Sacramento Rivers. Figure 21 illustrates that the largest volumes of Mount Shasta's ice are perched at the tops of these drainages, on the northern and eastern parts of the mountain. Ninety-four percent of the area covered by snow and ice is above 10,000 feet of altitude. Figures 22 and 23 show ice volumes for radar-measured glaciers and ice areas by drainage as a function of altitude.

More information about geological hazards at Mount Shasta can be found in the report by Miller (1980).

## CONCLUSIONS

On each of the mountains studied substantial amounts of snow and ice exist within probable eruptive zones and should be considered as factors in all eruption-hazard analyses. In times of eruption their role as hazards will depend on the extent of seasonal snow cover and eruption characteristics.

Glacier sizes and locations vary greatly on the volcanoes, depending on the local climate and each mountain's topographic configurations. Mount Rainier, the highest and farthest north of the volcanoes, has by far the largest and most well developed valley glaciers and snow patches. The Three Sisters and Mount Shasta have only one major valley glacier each—Collier and Whitney Glaciers, respectively. Mount Rainier's size is reflected in its large snow and ice volume (156.2 billion  $\text{ft}^3$ ), when compared to those of Mount Hood (12.3 billion  $\text{ft}^3$ ), Mount Shasta (4.7 billion  $\text{ft}^3$ ), and the Three Sisters (5.6 billion  $\text{ft}^3$ ).

The methods of volume estimation used in this study were developed by using relations derived from the ice-radar measurements of glaciers. The methods have been tested on glaciers with known volume and found applicable and valuable for use on glaciers of Cascade volcanoes in Washington, Oregon, and northern California. However, because glacier area and shear stress relations may vary with climate, it is important that care be taken in determining the suitability of the methods to glaciers elsewhere. The choice of using an area or a basal shear stress correlation is as important as determining the geographical suitability of a glacier. Glaciers not well defined in length and continuity may require some forethought and preliminary estimations of volumes before final estimations are made.

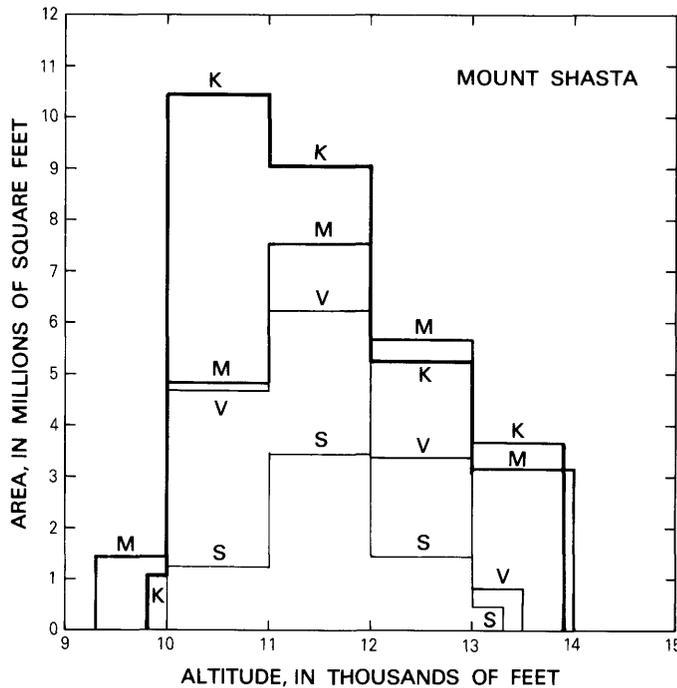


FIGURE 21.—Areas of ice and snow in each drainage basin of Mount Shasta as a function of altitude. Drainage basins listed are as follows: Klamath (K), McCloud (M), Sacramento (S), and a valley basin near the Whaleback Mountain (V).

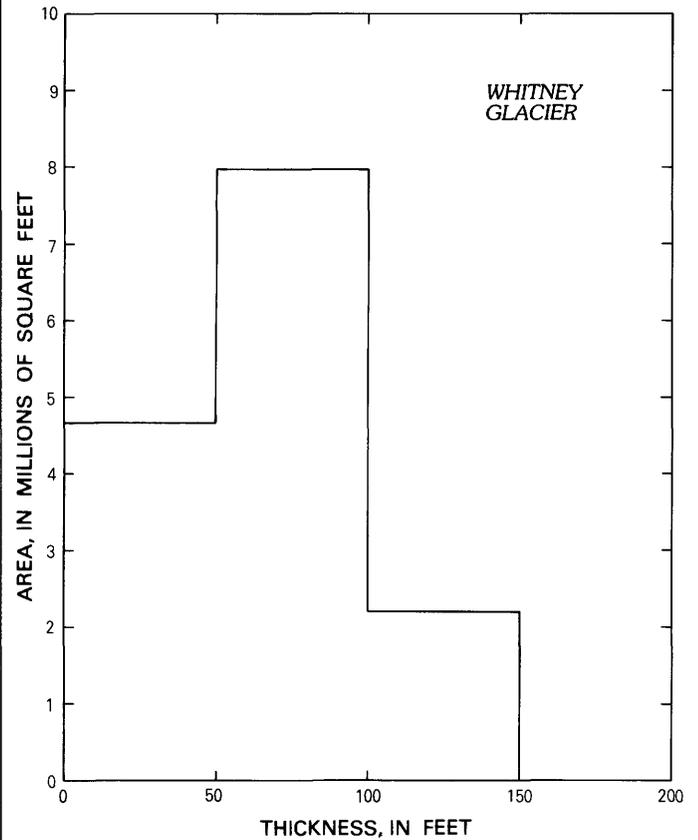
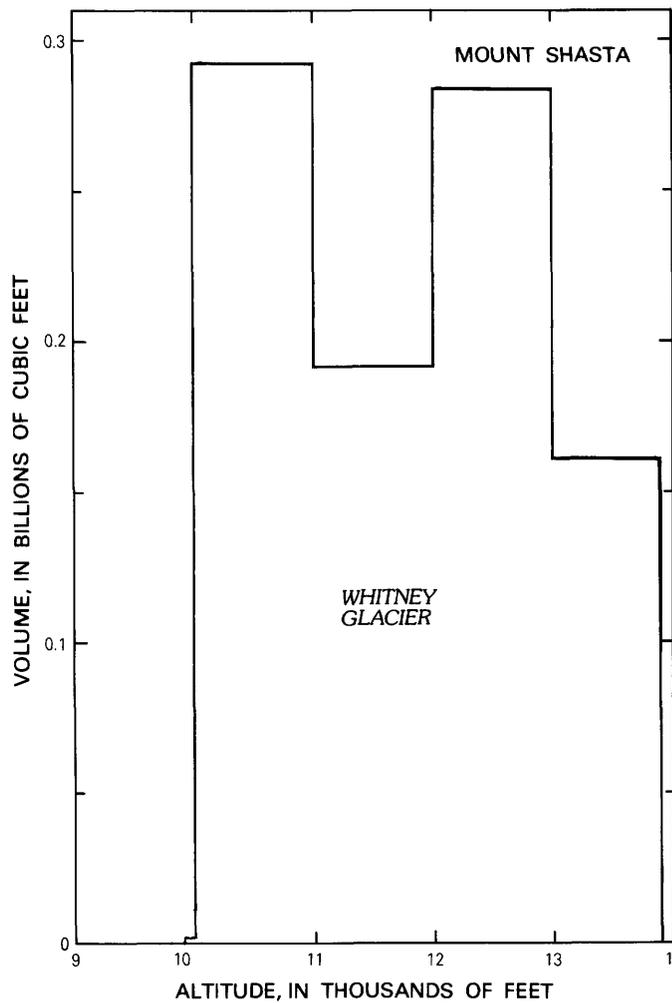


FIGURE 23.—Area of ice for selected thickness intervals on Whitney Glacier. Values are derived from isopach map.

**APPENDIX ON MONOPULSE RADAR**

The comparatively extreme electrical resistance and homogeneous nature of ice has allowed successful radar sounding through several miles of polar ice (Fitzgerald and Peran, 1975, p. 39). Until recently, similar success had eluded researchers in their efforts to sound temperate glaciers (glaciers having ice at the pressure melting point). The main problem encountered is the scattering caused by water found in temperature glaciers, not the increased electromagnetic absorption in the ice due to higher temperatures. Thus, the signal-to-noise ratio cannot be increased by improving system performance (Smith and Evans, 1972, p. 133). The ratio of radio wavelength to effective scat-

FIGURE 22.—Ice volume as a function of altitude on Whitney Glacier, the only glacier measured successfully by radar on Mount Shasta.

terer radius is recognized to be the controlling factor, and theoretical analysis shows that, if scattering is to be brought down to an acceptable level, the frequency must be reduced to 5 MHz or lower (Watts and England, 1976, p. 46).

Conventional radio detectors are tuned receivers, measuring a rectified electric field at a single frequency as a function of time. Therefore, several cycles of the carrier frequency need to be received in order to generate a response. As a frequency of 5 MHz corresponds to a wavelength of more than 100 ft, this resolution is inadequate for many temperate glaciers.

In theory this problem can be circumvented by use of a monopulse source at the correct frequency and an untuned receiver, which measures an unrectified electric field as a function of time. In this way, arrival times of the reflected wave could be picked within the accuracy of a small fraction of a single cycle (Watts and England, 1976, p. 40).

The technical breakthrough in application of these ideas was achieved by Roger S. Vickers and R. Bollen (1974, p. 2) and tested by them at South Cascade and Columbia Glaciers. Nondestructive avalanche transistor transmitters provided the necessary monopulse, and resistively loaded antennas eliminated the resonance problem (Watts and England, 1976, p. 40). Subsequent refinements resulted in the portable field unit used in this study.

#### APPLICATION

A thorough treatment of a similar system has been published (Watts and Wright, 1981), so only a basic outline of the instrument circuitry is provided, except where differences merit detail.

The principal components of the ground-based monopulse radar are schematically depicted in figure 24.

The two power supplies consist of 12-volt, rechargeable battery cells with gelatinized electrolyte. Of the two main parts, the receiving oscilloscope has the heavier power requirement, but in no instance was more than one battery change in a working day needed.

The specific transmitting circuitry was designed by David Wright, modified by Steven Hodge, and built by Robert Jacobel under the auspices of the Geological Survey. Circuit diagrams are available from the Geological Survey's Project Office—Glaciology. The antenna design was done by G. C. Rose and R. S. Vickers (1974, p. 261) and modified for field use by Steven Hodge (U.S. Geological Survey, written commun., October 1978).

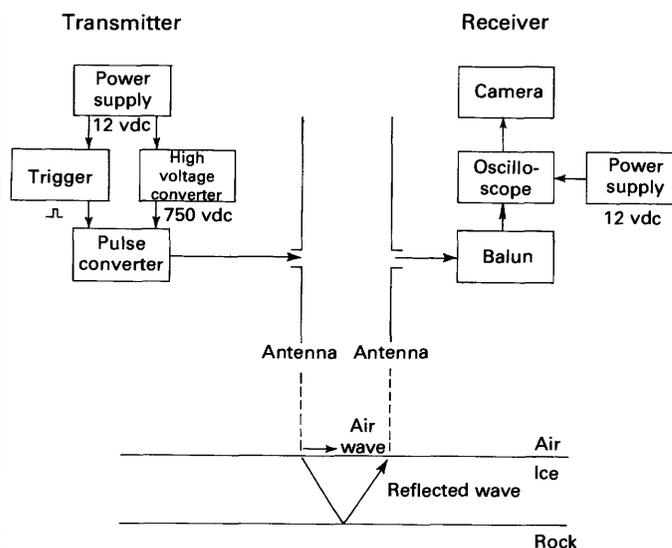


FIGURE 24.—Schematic diagram of the radar system used in this study (Kennard, 1983).

The transmitting power supply energized a trigger circuit and a high-voltage direct-current source. The trigger controlled the repetition rate (as distinct from the frequency) of the transmitted monopulse. This rate was variable over two ranges, 0.1 to 12.8 kHz. The oscilloscope recorded both the transmitted (air) wave, returns from intraglacial scattering, and the reflection from bedrock. Thus, the repetition rate needed regulation so that a subsequently transmitted wave would not obscure an earlier reflected wave.

The brightness of the oscilloscope trace is proportional to the repetition rate, which is an important factor in a sunlit field situation. Power consumption was increased with higher pulse rates but still never approached that of the receiver. A repetition rate of 10 kHz was generally used.

The power supply was a low to high voltage converter that supplied the necessary power for the transmitted pulse. A 750-volt, 20 mA capacity converter sufficed for the pulse generator configuration at the repetition rates used.

The pulse generator consisted of a variable number of avalanche transistor stages. Increasing the number of stages increased the amplitude of the transmitted pulse, until it was limited by the high-voltage supply and the thermal-dissipation capabilities of the transistors. Three configurations were tested: low power (2 stage), medium power (3 stage), and high power (4 stage). The optimal unit for these studies seemed to be the medium power pulse, which produced 600-volt pulses into a 50- $\Omega$  load. The low-power unit produced approximately 40 percent less power (Jacobel and Raymond, 1984) but caused no problem when used in the field. The high-power unit did not produce significantly more output but did draw more current.

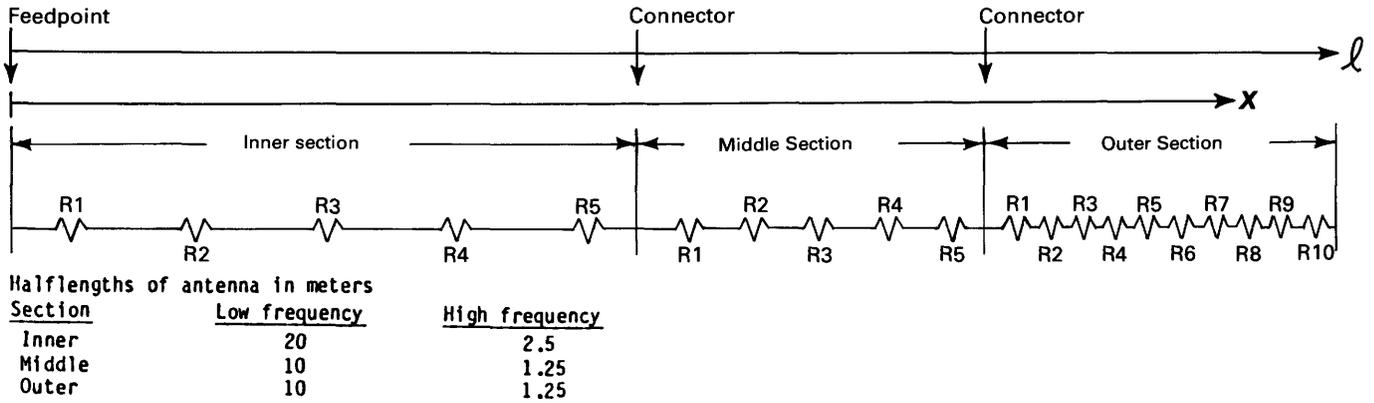


FIGURE 25.—Diagram of antenna illustrating positioning of resistors in the radar antenna. (Diagram from written communication, S. M. Hodge, U.S. Geological Survey, October 1978). To determine the required values of resistors in the outer antenna section, the antenna is divided into 10 intervals. Resistance is calculated where

$$\Delta R_{ab} = \int_a^b (\psi/Z) dZ = \psi \ln Z \Big|_a^b$$

$Z = l - x$ , where  $l$  is the antenna half-length, and  $x$  is the distance from the antenna feedpoint.  $R$  values for the inner middle sections equal values for  $R1$  through  $R5$  in the outer section. Half-lengths for high and low frequency antennas are also shown.

When a stage avalanched, it produced a fast voltage rise time (several tens of nanoseconds) and then returned to a high impedance state. The discharge current was limited by the antenna impedance, so the avalanching was nondestructive.

The final component of the transmitter system was the resistively loaded antenna, which was identical to the receiving antenna. The center frequency of the transmitted pulse (limited by the pulse generator) is a function of the antenna length and a resistive loading constant ( $\psi$ ). When the antenna is lying on an ice surface, the frequency is given approximately by the equation

$$v = 50/l' \quad (10)$$

where  $v$  is in megahertz and  $l'$  is the antenna half-length in meters.

To prevent ringing of the pulse produced by the transmitter the antenna is loaded according to the relation

$$R(x) = \psi/(l'-x) \quad (11)$$

where  $R$  is resistance per unit length at distance  $x$  from the feed point, and  $\psi$  is a constant in ohms. The constant,  $\psi$ , affects the pulse duration and the radiated power. Increasing  $\psi$  decreases the duration of the pulse (increasing resolution) but also decreases the radiated power. In practice, the variation is not critical, and in applications where increased power is needed, such as in thick ice, the decrease in resolution is usually acceptable.

The two main criteria for antenna design are the length, which determines frequency, and the resistive loading, which determines resolution and power. In this study, two basic configurations were chosen with respect to frequency: the high and the low. Because frequency is a function of antennas length only, it can be changed by simply removing or adding center sections of the antenna. If the section lengths are chosen as shown in figure 25, only 10 discrete resistor values are required for a given  $\psi$  value, and one antenna design is thus capable of producing pulses at six different frequencies (Steven Hodge, U.S. Geological Survey written commun., October 1978).

The antennas used on the project were  $\psi = 400 \Omega$  (low frequency) and  $\psi = 1,500 \Omega$  and  $2,500 \Omega$  (high frequency). In testing antennas, it has been found that the outer arms alone (10 m, 5 MHz) of the low frequency antennas give the best results on the relatively thin, temperate glaciers of the Cascade Range and were the easiest to operate. These tests were not comprehensive, yet it was found that if a good bottom reflection could not be achieved with the low-frequency set, it could not be achieved with the high-frequency set. This result was not surprising, considering the expected signal scattering in temperate glaciers. Generally, in this study the 400- $\Omega$  antennas were used.

The transmitted signal was about  $10^6$  times stronger than the received signal, necessitating the use of separate but identical antennas. The receiving antenna impedance was matched to the oscilloscope with a balun. Optimal input:output voltage and impedance ratios (Hodge, U.S. Geological Survey, written com-

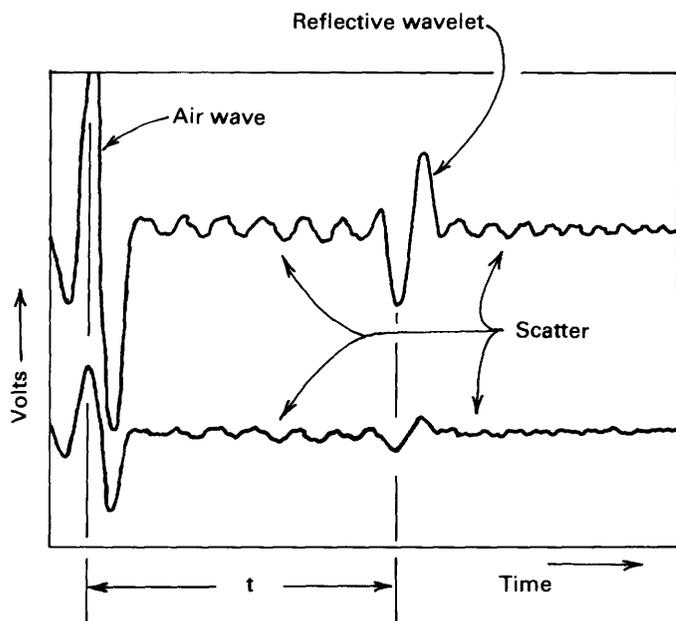


FIGURE 26.—Oscilloscope output. Air wave and reflected wavelet as seen on the oscilloscope screen. Quick-developing photographs were taken at the traces at each measurement point. The time interval between wave transmission and receipt is expressed as  $t$ . Two traces were set at differing amplitudes to accent features in the air wave and the reflected wave.

mun., October 1978) were found to be 3:1 and 9:1, respectively. Others have also used a preamplifier (for thick ice) and a bandpass filter (1–10 MHz) at this stage (Watts and Wright, 1981, p. 460), though these were not required in this fieldwork.

The oscilloscope constitutes the core of the receiving system. A band width of 30 MHz is used, and the unit is otherwise chosen according to power requirements, weight, sensitivity, and trace brightness.

The oscilloscope trace is triggered by the incoming air wave and records this wave and the reflected wavelet (fig. 26). A two-channel oscilloscope is preferable because the incoming signal can be viewed at two different amplification levels. In this way, a relatively strong air wave and a reflected wave can be viewed in detail simultaneously.

The trace output was recorded by an oscilloscope camera on self-developing film. Minimizing light leaks and maintaining the film at higher-than-ambient temperature were the only difficulties encountered.

The layout geometry of the antenna at each measurement point depended on the ability of a particular configuration to give an unambiguous bottom return. Figure 27 shows the primary antenna layouts used on the glacier. In general, the parallel configuration (A) was tried first. The air-wave used to trigger the scope is of predictable polarity and there is maximum coupling of the antennas. An attempt was made to align the anten-

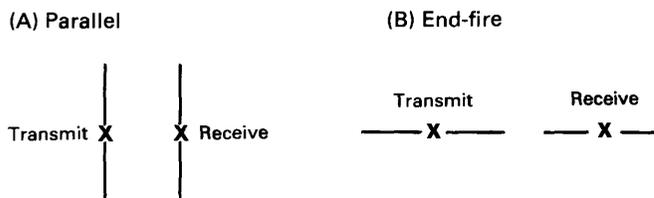


FIGURE 27.—Typical antenna configurations used during measurements. Placement was dependent on the clarity of a bottom return on the oscilloscope trace.

nas parallel to the expected bottom contours. If ambiguous returns continued, the separation distance between the transmitter and receiver antenna was changed.

If bottom returns were still unsatisfactory, the end-fire configuration (B) was used at various separations. Although the airwave coupling is decreased, the quality of bottom returns would occasionally be enhanced.

The obtaining of some successful bottom returns even with both or parts of the antennas hanging down crevasses, and, in one instance, coiled, indicates that the antenna configuration was not critical. The presence of surficial debris, crevasses of various orientations, water, or volcanic ash did not seem to have any effect on the success of receiving bottom returns. In general, if a satisfactory bottom return was not found in an area, it was necessary to move at least an antenna-length away from the original measurement location.

As the air wave triggers the oscilloscope, it is necessary to know the transmitter-receiver separation in order to determine the total travel time of the reflected wave. First seen on the left side of the scope trace is the air wave.

A surface wave also travels directly through the ice and usually appears as a minor disruption of the airwave. Next are returns of scattered signals from ice inhomogeneities, finally followed by the reflected wave, which has undergone a phase reversal.

For depth determination, the information of interest is the time delay ( $t$ ) between a point on the airwave and a corresponding point on the reflected wave. Because frequency is not necessarily preserved between the air and reflected waves, it is most accurate to choose this point to be early along the pulse. Almost exclusively the first peak was chosen (whether of positive or negative amplitude) to be the basis for calculation of the time delay.

For purposes of this study, the only concerns were the respective positions of the air and reflected waves. It is possible that useful information about the nature of englacial scatterers can be obtained from further study of the remainder of the recorded signals (Jacobel and Raymond, 1984).

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## CONVERSION FACTORS

For readers who prefer International System (SI) units, conversion factors for terms used in this report are listed below. Except where required by use with maps, stresses are expressed in bars ( $10^5$  Pascals), a preferred unit in glaciology.

Multiply inch-pound unit	By	To obtain SI unit
foot (ft)	0.3048	meter (m)
square foot (ft <sup>2</sup> )	0.0929	square meter (m <sup>2</sup> )
cubic foot (ft <sup>3</sup> )	0.0283	cubic meter (m <sup>3</sup> )
mile (mi)	1.609	kilometer (km)
square mile (mi <sup>2</sup> )	2.590	square kilometer (km <sup>2</sup> )
cubic mile (mi <sup>3</sup> )	4.168	cubic kilometer (km <sup>3</sup> )
pounds per square foot (lb/ft <sup>2</sup> )	$4.787 \times 10^4$	bar
slugs per cubic foot (slug/ft <sup>3</sup> )	1.187	kilogram per cubic meter (kg/m <sup>3</sup> )

Water equivalence:

$$\text{Volume of water in cubic feet} = \frac{\text{Volume of ice in cubic feet (1.8 slugs/ft}^3\text{)}}{1.94 \text{ slugs/ft}^3}$$

In this study, inch-pound units have been used to be compatible with the most current U.S. Geological Survey topographic maps.

